Imperial College London



Big Data and the evolving many-core landscape: Are traditional low level programming models really enough?

Gerard Gorman, Imperial College London

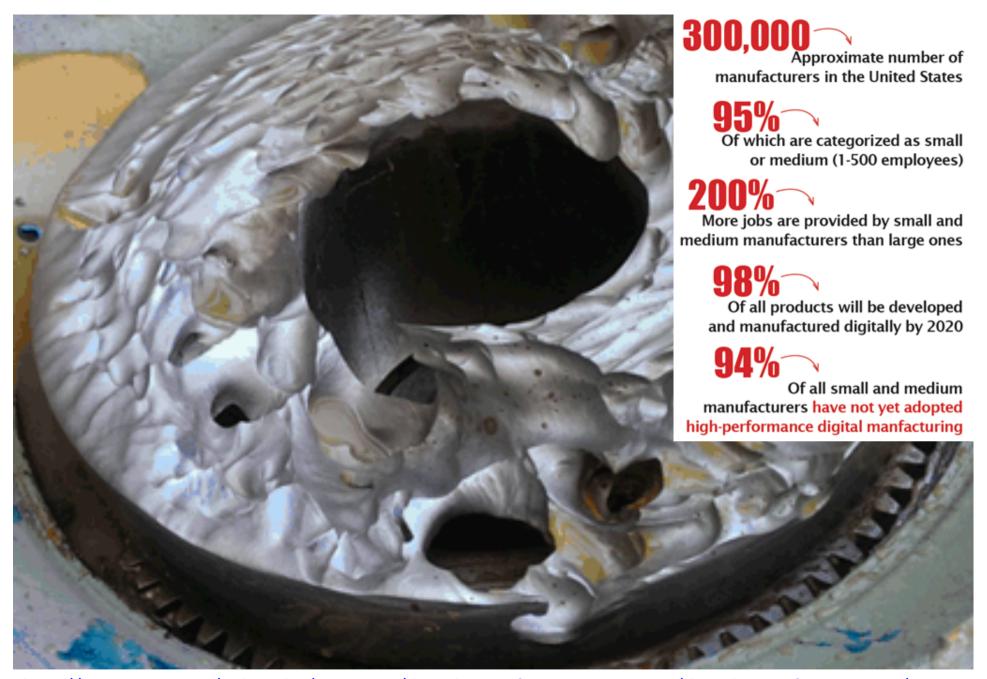
Intel Parallel Computing Center
Open Performance portablE SeismiC Imaging









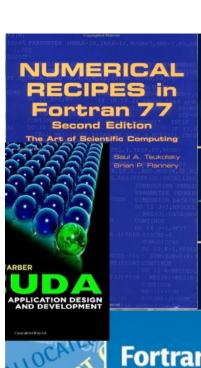


http://www.ncms.org/index.php/programs/digital-manufacturing-initiative/digital-manufacturing-sig/

HPC often compared to F1... ...the problem is that the comparison is accurate.



Original: https://www.youtube.com/watch?v=EGUZJVY-sHo



O.C. ZIENKIEWICZ & R.L. TAYLOR
The
FINITE ELEMENT
METHOD



FORTHAN
INPUT: REASON • OUTPUT: PLEASURE

Volume 1 THE BASIS

FIFTH EDITION



NUMERIC RECIPES i

The Art of Scientific Cor

William H. Press Saul A. To William T. Vetterling Brian P. F



OpenCL Programming by Example

A comprehensive guide on OpenCL programming with examples

Ravishekhar Banger Koushik Bhattacharyya PACKT



iplates Stephen Randy Davis Stephen Randy Davi

DUM

Rest of Us!

mytype

rn Fortran explained







SOFTWARE-ENVIRONMENTS-TOOLS





The Complete Reference

subroutine
class(mytype)
integer.optional :: Uni
if (present(unit)) then
write (unit,*) thisknyvalue
else MICHAEL METCALF
print *.th.JOHN REID
end if MALCOLM COHEN
end subroutine write mytype
subroutine wrace lyestable)

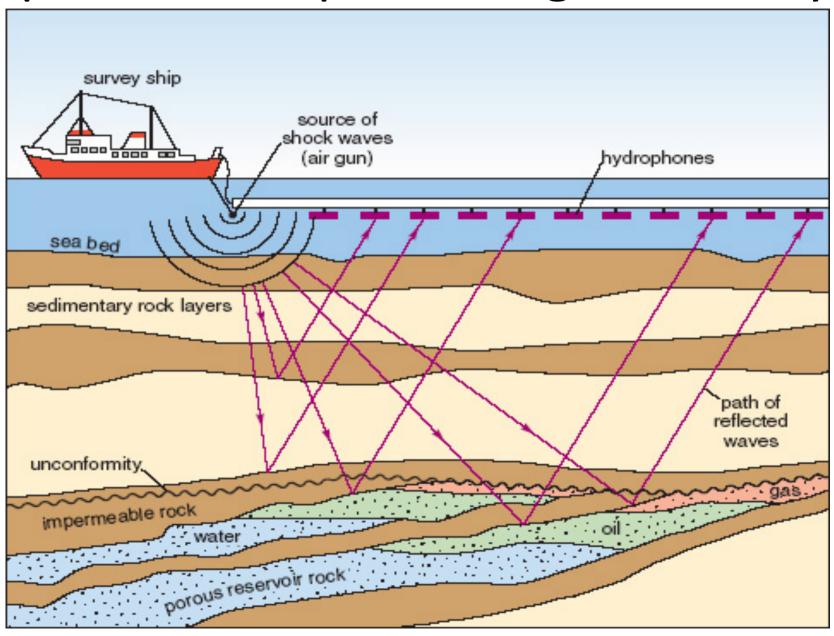
class(mytype) :: variable)
variable)mytype) :: variable
variable)mytydde : 0.0
end subroutine : OXFORD

SC14 Registration Count 2014-Nov-10

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Specific example – oil&gas industry



Full Waveform Inversion

- Given a sound source, and an array of receivers, can we infer the subsurface?
- Yes but it is computationally expensive:
 - Lots of data, terabytes per survey (this is a real Big Data problem!)
 - Dominant computational expense is running the wave model (aka forward model, and propagator) for each shot of data.
 - Regardless of how good the inversion algorithm is, the quality of the final subsurface image will be limited by the accuracy of the wave model used.

Opportunity & challenge I Elastic wave equation (Improved model)

- Elastic wave model provides a significantly better representation of the wave field than the standard acoustic models.
 - Models both p-waves, s-waves and Rayleigh waves.
- It is also much more expensive to compute:
 - More terms in the equation to compute.
 - S-waves travel at about half the speed of p-waves, and there have half the wavelength, therefore:
 - Grid resolution needs to be doubled (factor of 8 increase in memory for 3D).
 - Time step needs to be halved therefore must execute twice the number of time steps.

Opportunity & challenge II Advanced numerical methods

- Regular grids with finite difference is the modus operandi of oil and gas industry.
- However:
 - Unstructured grids are more efficient at representing complex geological features.
 - High order methods can achieve the same accuracy as finite difference methods using:
 - Coarser resolution (fewer grid points).
 - Larger time step.
 - Less memory.
 - Shorter time to solution.
 - Great data locality, opportunities for vectorisation etc.
- Best example from global seismic: SeisSol Arbitrary high-order DERivative Discontinuous Galerkin (ADER-DG), 2014 Gorden Bell finalist.
- Implementation complexity!
 - A lot more software is required to manage unstructured grids.
 - Impacts entire inversion software stack.
 - High order methods are many times more involved finite difference methods.

Opportunity & challenge III Architecture and code modernisation

- Computing performance continues to track Moore's Law but you have to work harder to make use of it.
- Many-core era software must exploit parallelism at every level to achieve good computational efficiency, e.g.:
 - Various parallel programming models (MPI, OpenMP/pthreads, OpenCL, OpenMP, Cilk, etc.)
 - Deep memory hierarchy, data locality.
 - Vectorisation (AVX).
 - Heterogeneous computing Intel Xeon, Xeon Phi, etc.
- Parallel programming has always been considered challenging and now it has become over more demanding:
 - Greater need for specialists in parallel programming for HPC.
 - Increasingly difficult for domain specialists to implement high performance software although they are the algorithm specialists.
 - Traditional numerical algorithms may need to be discarded in favor of methods better suited to computer architectures.
- Domain Specific Languages (DSL's) offer a route to bridge the divide between domain specialists (often the application developers) and parallel programming specialists (in this case compiler writers).

Inversion algorithm (High level language such as Python, MATLAB or Julia) Geophysicist Nonlinear gradient-based optimization methods; compressive sensing (randomised sparse sampling) Forward models written using DSL: 2D/3D; acous-Numerical tic/elastic wave equation; isotropic/anisotropic Backward (adjoint) model (Code generation) analyst elastic modulii; and time/frequency domain Gradient&Hessian operators (Code generation) Reference implementation of kernels (Fortran, C, etc.) Library, and Iterative solvers (PETSc with do-DSL compiler Stencil DSL for finite difference (Pochoir) main specific optimisations) developers Seismic data I/O module (SEG-Y) with exten-UFL for finite element (Firedrake) sions to support randomised sampling; High throughput checkpointing module for inversion Platform specific data layouts and task scheduling; Anisotropic adaptive meshes code generation for MPI with OpenMP or OpenCL **Platform** Platform tuned kernels; autotuning frameworks MPI, OpenMP, OpenCL specialist x86_64, Intel Phi, GPGPU etc. Future architecture

UFL/Firedrake



Domain developer: expert in application field



Numerical analyst: expert in finiteelement

methods

al

An expert for each layer



Domain developer: abstractions not expressible



in UFL

Computer scientist: expert in parallel programming, optimisation

Unified Form Language (UFL)

Domain-specific language developed by the FEniCS project: high-level description of weak forms of PDEs, very close to mathematical notation

UFL code

UFL Code Generation Engine

Implements local assembly strategies for finite element forms: breaks the link between numerical problem specification and algorithmic implementation

Local assembly kernels and data dependencies

OP2 Interface

Abstraction for the specification of explicit parallel loop computations declared over an abstract data representation of unstructured meshes

> Parallel loops over kernels with access descriptors

OP2 Transformation/Scheduling

Implements threading, colouring, message passing, data marshalling for different platforms: breaks the link between algorithmic and parallel implementation

A weak form of the shallow water equations

$$\int_{\Omega} q \nabla \cdot \mathbf{u} dV = -\int_{\Gamma E} \mathbf{u} \cdot \mathbf{n} (q^{+} - q^{-}) dS$$

$$\int_{\Omega} \mathbf{v} \cdot \nabla h dV = c^2 \int_{\Gamma E} (h^+ - h^-) \mathbf{n} \cdot \mathbf{v} dS$$

can be represented in UFL as

UFL source

```
V = FunctionSpace(mesh, 'Raviart-Thomas', 1)
H = FunctionSpace(mesh, 'DG', 0)
W = V*H
(v, q) = TestFunctions(W)
(u, h) = TrialFunctions(W)
M_u = inner(v, u) *dx
M_h = q*h*dx
Ct = -inner(avg(u), jump(q,n)) *dS
C = c**2*adjoint(Ct)
F = f*inner(v, as_vector([-u[1], u[0]])) *dx
A = assemble(M_u+M_h+0.5*dt*(C-Ct+F))
A_r = M_u+M_h-0.5*dt*(C-Ct+F)
```

Local assembly kernel

```
void Mass(double localTensor[3][3])
{
  const double qw[6] = { ... };
  const double CG1[3][6] = { ... };
  for(int i = 0; i < 3; i++)
    for(int j = 0; j < 3; j++)
    for(int g = 0; g < 6; g++)
        localTensor[i][j]
        += CG1[i][g] * CG1[j][g] * qw[g]);
}</pre>
```

parallel loop over all grid cells,

in unspecified order, partitioned

unstructured grid defined by vertices, edges and cells

Explicitely parallel hardware-specific implementation

Multicore CPU + MPI

GPU + MPI

Future hardware

Abstraction facilitates automatic differentiation of models



The Wilkinson Prize was established to honour the outstanding contributions of Dr James Hardy Wilkinson to the field of numerical software. It is awarded every four years at the International Congress on Industrial and Applied Mathematics by Argonne National Laboratory, the National Physical Laboratory, and the Numerical Algorithms Group. The recipients are authors of an outstanding piece of numerical software, judged on:

- the clarity of the software implementation and documentation;
- the importance of the application(s) addressed by the software;
- the portability, reliability, efficiency and usability of the software implementation;
- the clarity and depth of analysis of the algorithms and the software in the submission;
- the quality of the test software.



The 2015 prize is awarded to <u>P.E. Farrell</u> (University of Oxford), <u>S.W. Funke</u> (Simula Research Laboratory), <u>D.A. Ham</u> (Imperial College London), and <u>M.E. Rognes</u> (Simula Research laboratory) for the development of <u>dolfin-adjoint</u>, a package which automatically derives and solves adjoint and tangent linear equations from high-level mathematical specifications of finite element discretisations of partial differential equations. The prize will be presented at ICIAM 2015 and will consist of \$3000 plus a commemorative plaque for each winner.

Example using UFL/Firedrake

• Velocity-stress formulation of elastic wave equation, with isotropic stress:

$$\rho \frac{\partial \mathbf{u}}{\partial t} = \nabla \cdot \mathbb{T} \tag{1}$$

$$\frac{\partial \mathbb{T}}{\partial t} = \lambda \left(\nabla \cdot \mathbf{u} \right) \mathbb{I} + \mu \left(\nabla \mathbf{u} + \nabla \mathbf{u}^{\mathrm{T}} \right) \tag{2}$$

• Weak form of equations written in the high-level Unified Form Language (Logg et al., 2012), e.g. (1):

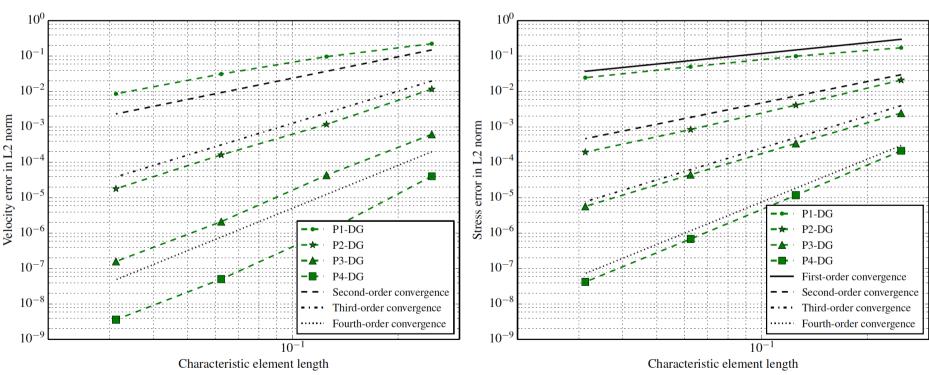
```
F_u = density*inner(w, (u - u0)/dt)*dx + inner(w, div(s0))*dx
```

 Change order of DG spatial discretisation with a 'flick-of-a-switch', e.g. P1-DG to P4-DG:

```
U = TensorFunctionSpace(mesh, "DG", 1) \rightarrow U = TensorFunctionSpace(mesh, "DG", 4)
```

• UFL compiled down to low-level, optimised C code, and targetted to specific hardware architecture.

- Simulation of an eigenmode to verify model correctness.
- Numerical solution compared with analytical solution at $T=5\,\mathrm{s.}$
- For degree d polynomial basis functions (d = 1,2,3,4) on increasing mesh resolutions, we observed O(d+1) convergence for velocity, O(d) for stress.
- ...Except for d=4 where the overall convergence was limited to 4th order because of 4th order leapfrog scheme.



Alternative approach - Stencil languages

- Good for applications such as finite difference, image processing (see conference proceedings for HiStencils).
- Automate the entire workflow with smart abstractions
 - Python/SymPy (high level, symbolic math).
 - Code generation to target stencil language, e.g. Pochoir.
 - Code generation from stencil language to native source code.
- High level retains expressiveness key to innovation.
- Extreme optimization techniques performed by the stencil compiler.
- Separation of concerns enables effective collaboration.

Conclusions

- To bring about disruptive change in areas such as data inversion and design optimization progress must be made on three fronts:
 - Better models.
 - Advanced numerical models.
 - Domain specific languages (DSL's) and code generation.
- A number of stencil compilers are already available for finite difference and performance results show that these already offer an attractive code modernization solution without impacting the rest of the software stack.
- Methods pioneered by SeisSol for global seismic inversion appears to offer the best numerical approach currently. A drawback with moving to these sophisticated methods is that they are challenging to implement – which raises issues for code optimization and sustainability.
- UFL and the Firedrake compiler facilitates a separation of concerns which allows application developers to develop these sophisticated schemes without any knowledge of the hardware, while compiler writers take these abstract forms and automatically generate native source code whose performance is competitive to what a human expert could achieve.

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 - Renato Miceli (Computing)
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 - Felippe Vieira Zacarias (Computing)



Links

- OPESCI http://opesci.github.io (Intel PCC)
- Firedrake http://www.firedrakeproject.org
- FEniCS http://fenicsproject.org
- Dolfin-adjoint http://www.dolfin-adjoint.org
- PRAgMaTIc https://github.com/meshadaptation/pragmatic
- PETSc http://www.mcs.anl.gov/petsc/
- PRISM http://prism.ac.uk
- AMCG http://amcg.ese.ic.ac.uk