



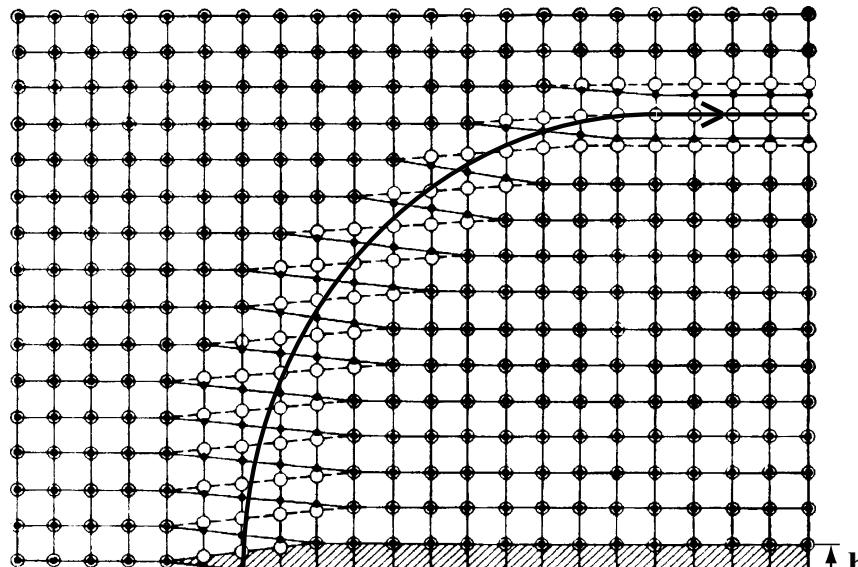
# The Discrete-Continuum Model: An important breakthrough to simulate the mechanical properties of crystalline materials

R. Gatti<sup>1</sup>, O. Jamond<sup>1,2</sup>, A. Roos<sup>2</sup>, B. Devincre<sup>1</sup>

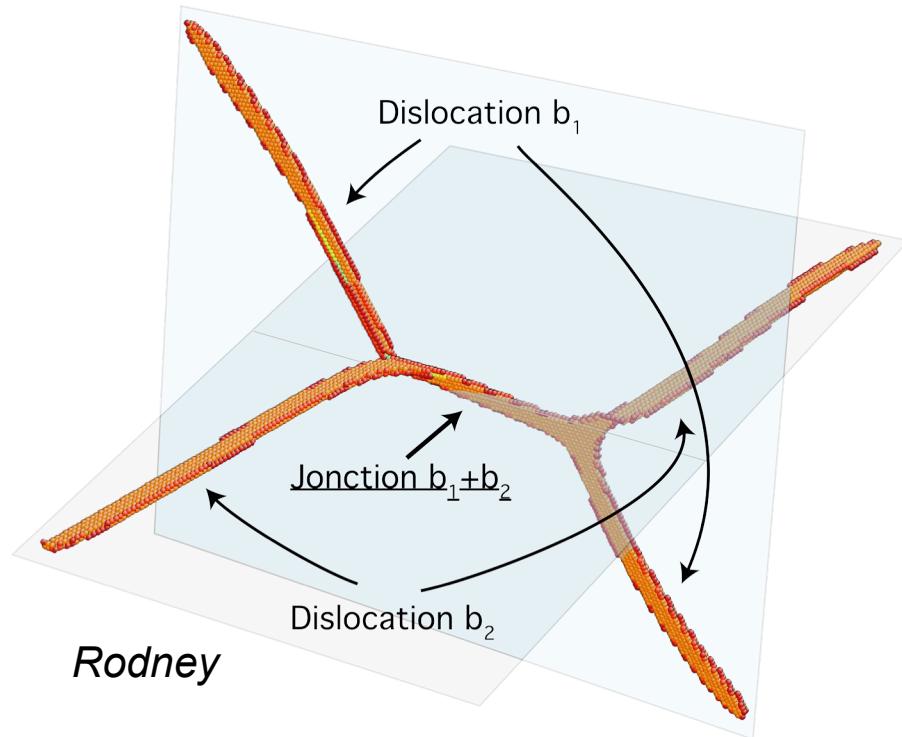
(1) LEM, CNRS–ONERA, 92322 Châtillon, France

(2) DMSM, ONERA, 92322 Châtillon, France

# Dislocations



Read(1953)



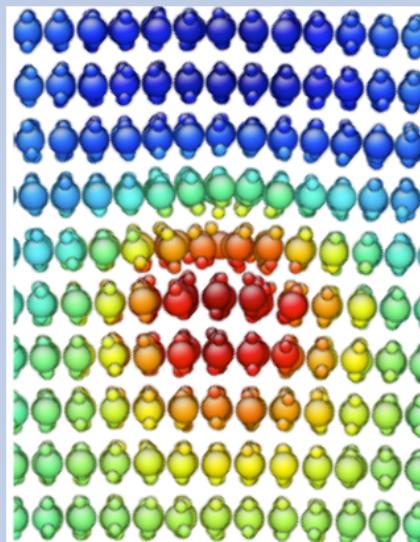
Rodney

- Linear crystalline defect
- Long range elastic field (singular at the line)
- Short range properties (core properties)
- A crystal contain a huge density of dislocations

# Multiscale modeling of plasticity

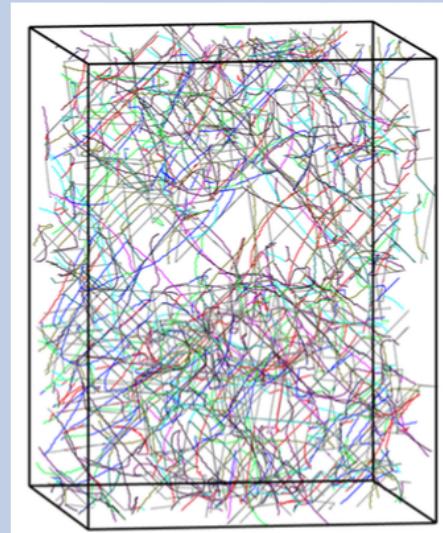
MD - MS - etc..

nm and  $10^{-15}$  s



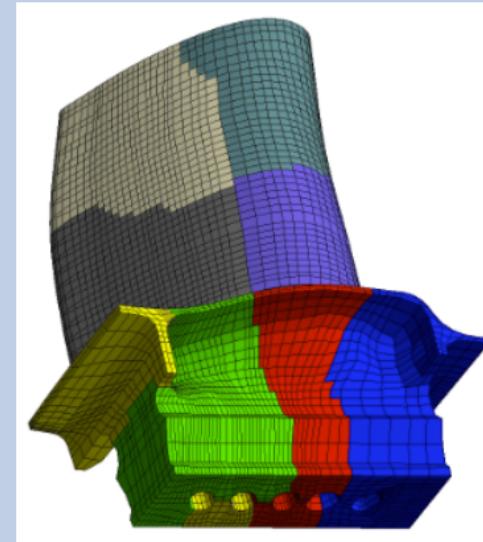
DD (DDD)

$\mu\text{m}$  and  $10^{-10} - 10^{-5}$  s



FEM - BEM - etc ...

mm - km and s - y



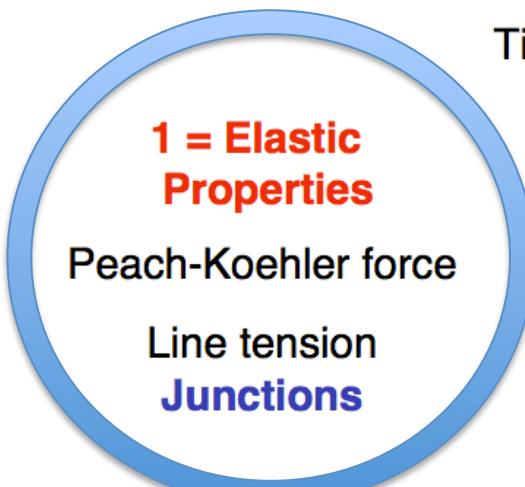
DD simulation is the Key element between discreet ( $\phi$ )  
and continuous (M) modeling of crystal plasticity

# Outplane

1. The Discrete-Continuous Model (DCM)
2. Performance analysis
3. Simulation examples
4. Concluding remarks

# 3D - Dislocation Dynamics Simulation

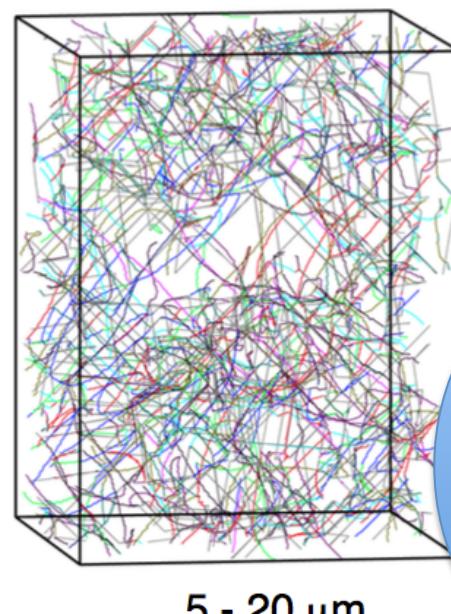
(*microMegas (mM) a free GPL code*)



**2 = Local rules**  
**Velocity-stress**  
**Cross-slip**  
**Climb**

Other crystal defects interac.  
(Grain boundary,  
precipitates...)

**Discretization**  
Time(  $10^{-6} - 10^{-15}$  s ) & Space ( 1 - 100 b )  
Line & Character



**3 = Initial conditions**  
Defects density  
Loading conditions

**4 = Boundary conditions  
(periodic or finite)**

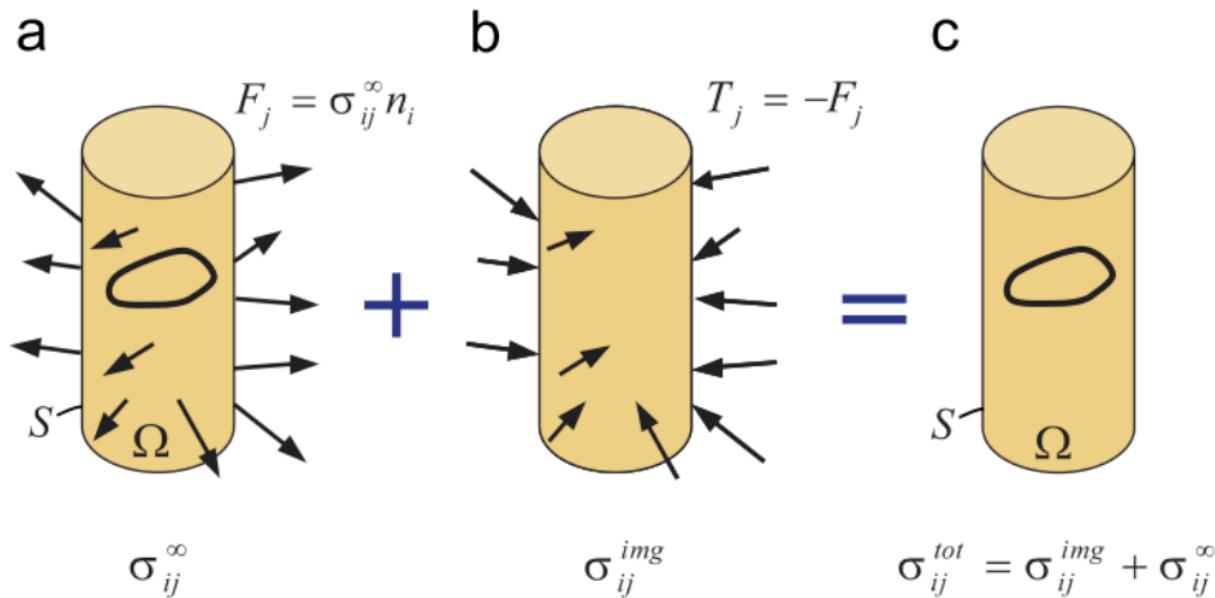
Dislocation flux  
Crystal equilibrium

+  
**Surfaces & interfaces**

FCC, BCC, HCP, DC,  
orthorhombic ...

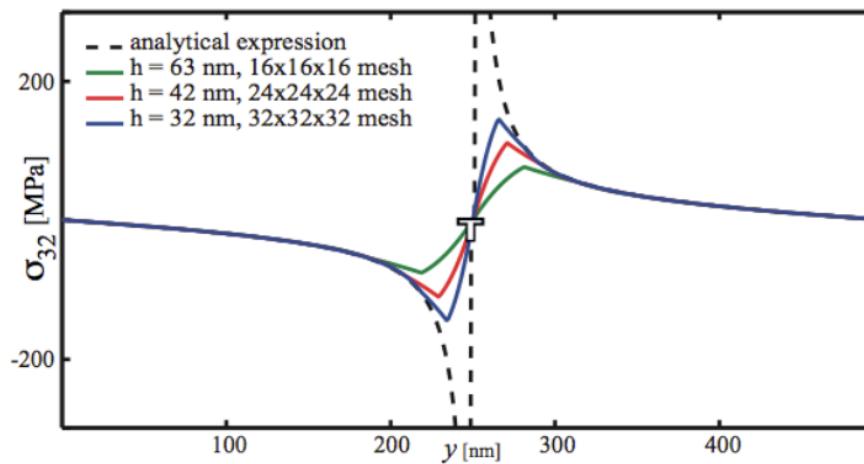
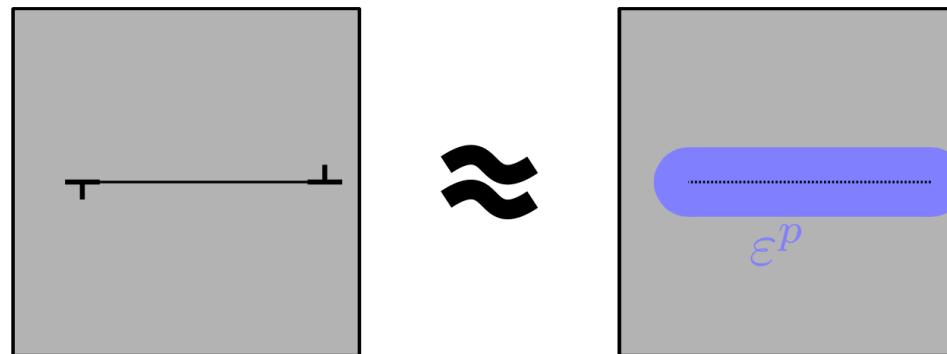
# Superposition method

- > 2D, van der Giessen and Needleman (1995); ...
- > 3D, Fivel; Weygand and van der Giessen, Weinberger and Cai; ...



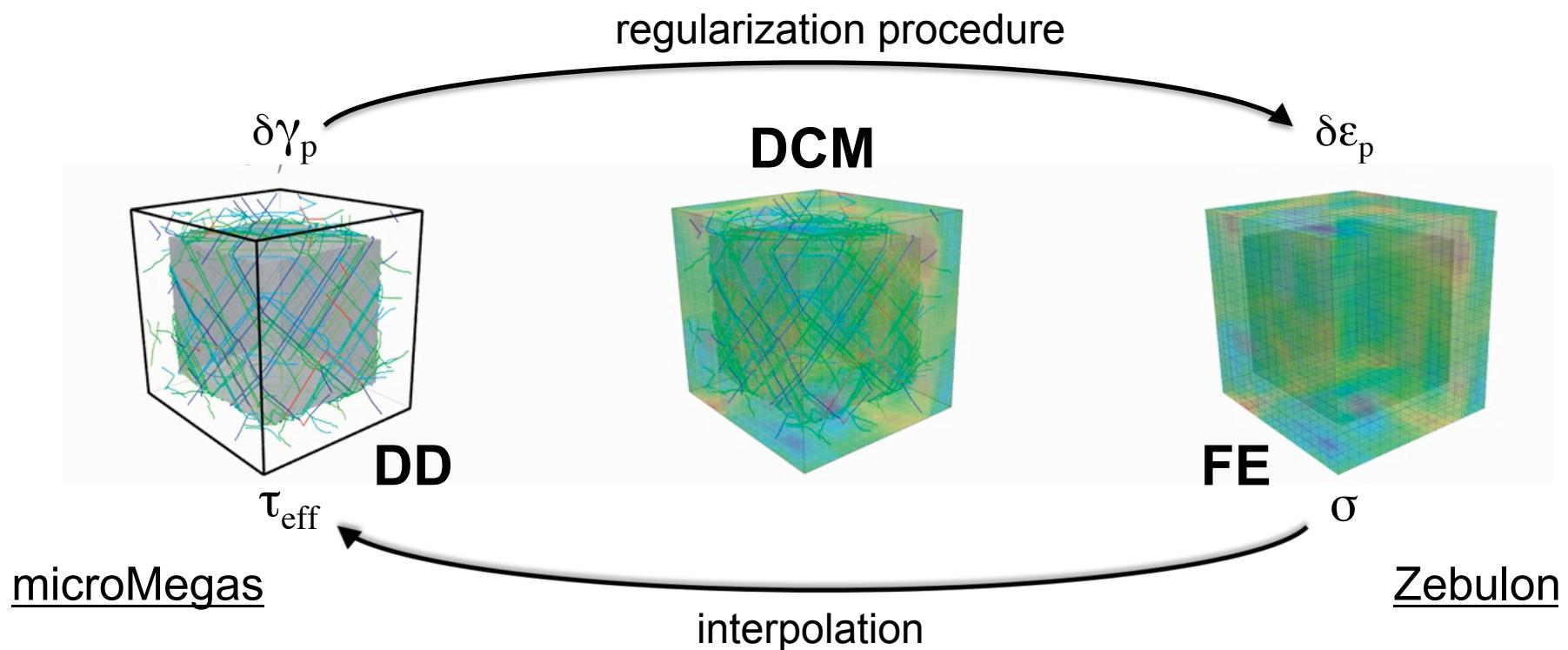
- Dislocation singular field is a problem at surfaces and interfaces
- Not adapted to simulate periodic systems

# Mura theory: Dislocation $\approx$ Eigenstrain



Need for a local correction in the DD code to handle  
for dislocation-dislocation short range interaction.

# The Discrete Continuum Model



- Short range interaction
- Dislocation microstructure

- Mechanical equilibrium
- boundary conditions
- Long range interaction

C. Lemarchand, J. L. Chaboche, B. Devincre, and L. P. Kubin. Multiscale modelling of plastic deformation. *J. Phys. IV*, 9:271, 1999.

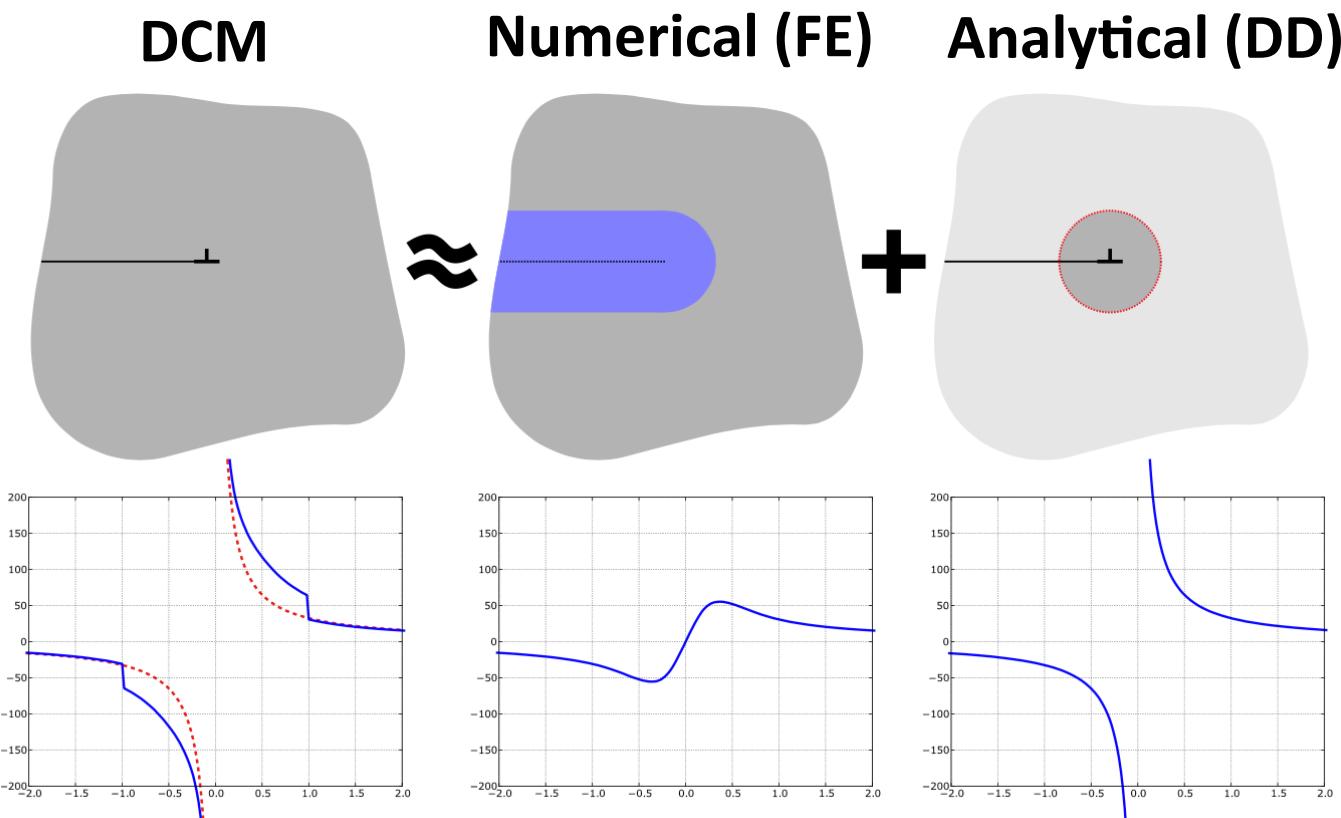
# The Discrete Continuum Model (V.2)

The model was revised in the last 2 years:  
(Post-Doc: O. Jamond)

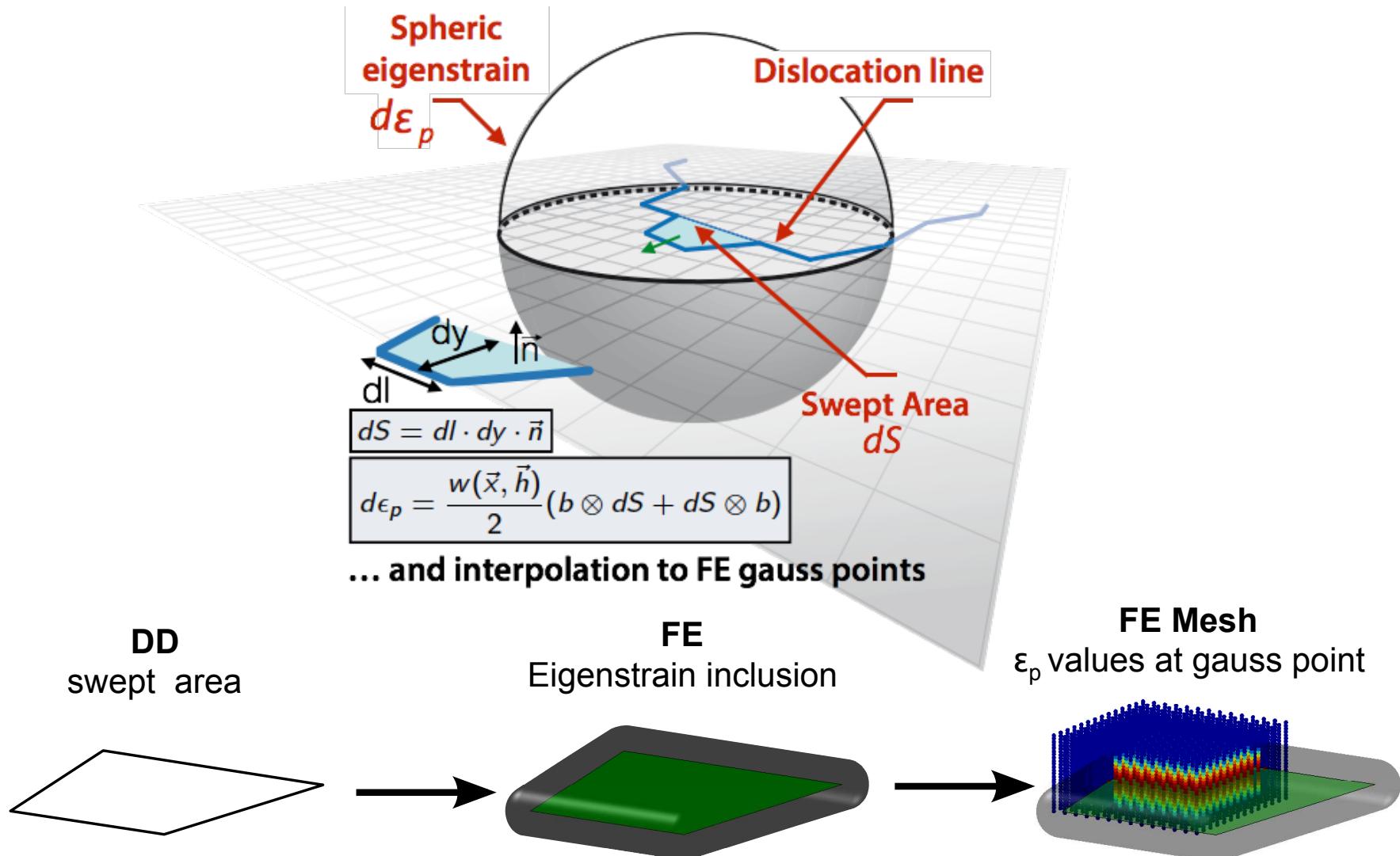
- New regularization procedure
- Unstructured meshes to run simulation in complex domains
- Performance and accuracy improvements
- New computation possibilities

# The DCM initial solution

Local analytical correction in the DD code to handle dislocation short distance interaction.

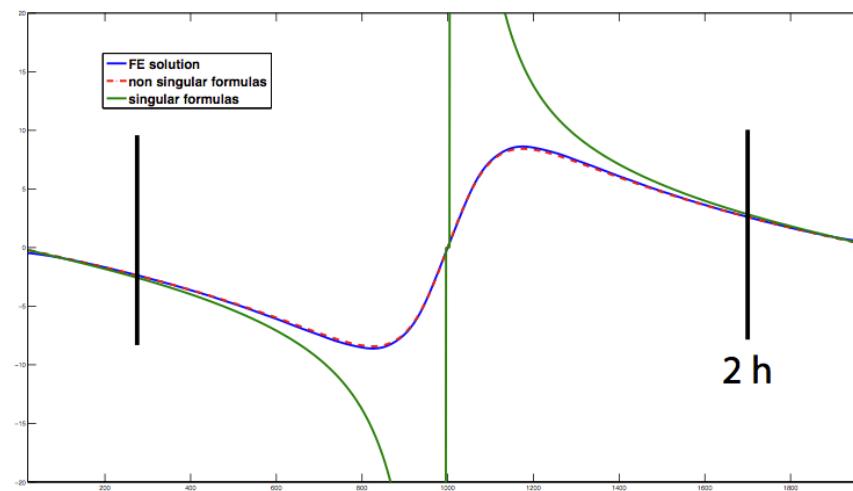
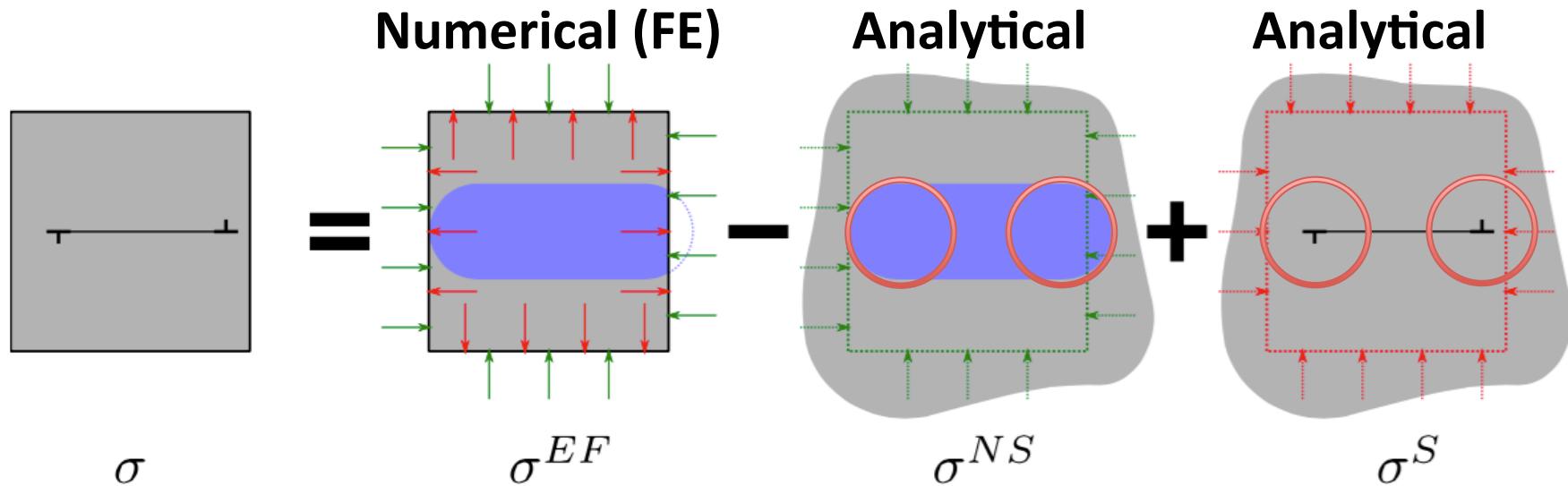


# DCM: New regularization procedure

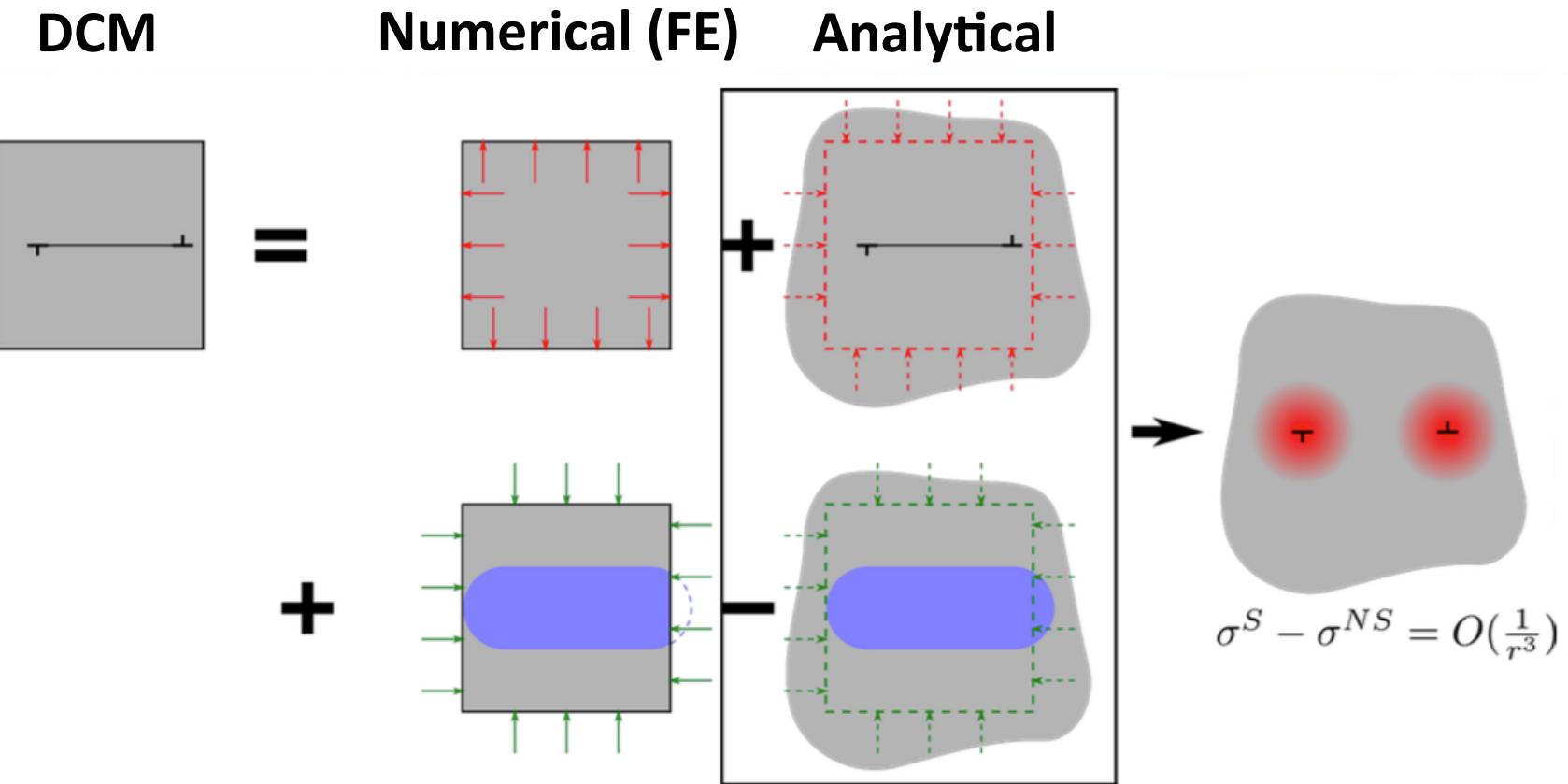


# The DCM new solution

The mechanical problem of dislocated solids is now exactly solved



# Main benefit of the new solution

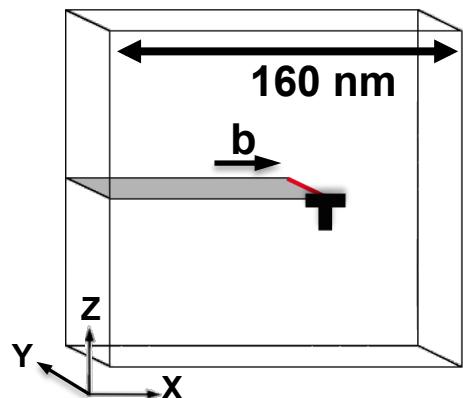


The difference between the two analytical fields is decreasing fast.  
Hence, the FE mesh can handle many dislocations in one element!  
The boundary value problem is more easily solved!

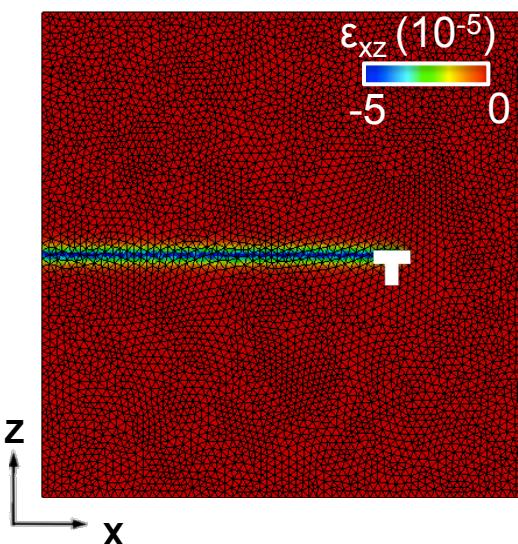
# DCM: unstructured meshes

Example: Infinite edge dislocation interacting with 4 free surfaces

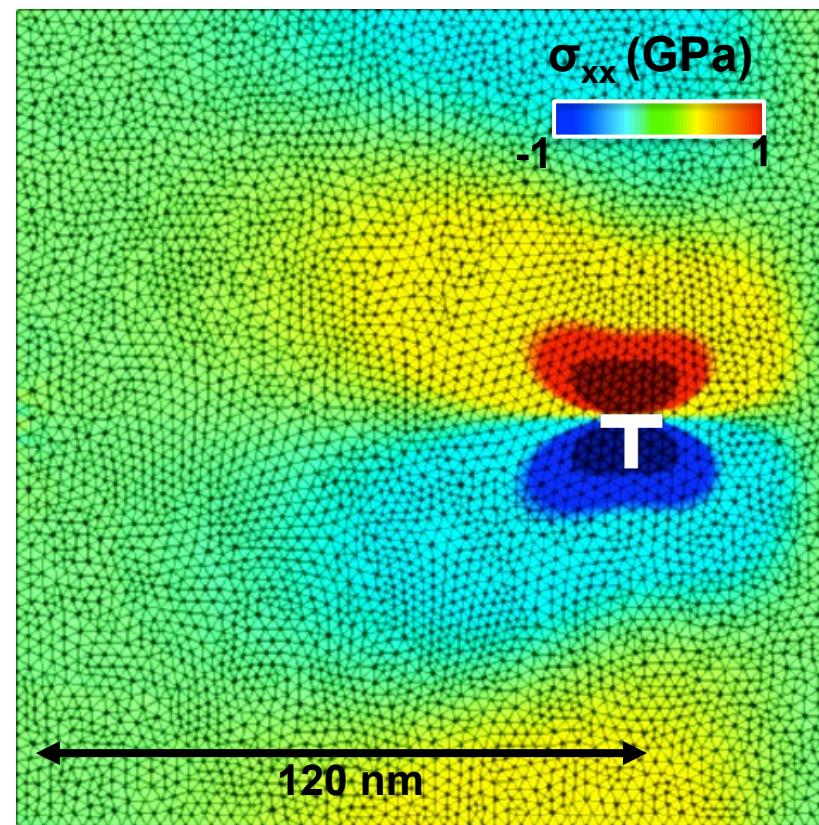
Simulation settings



Plastic eigenstrain



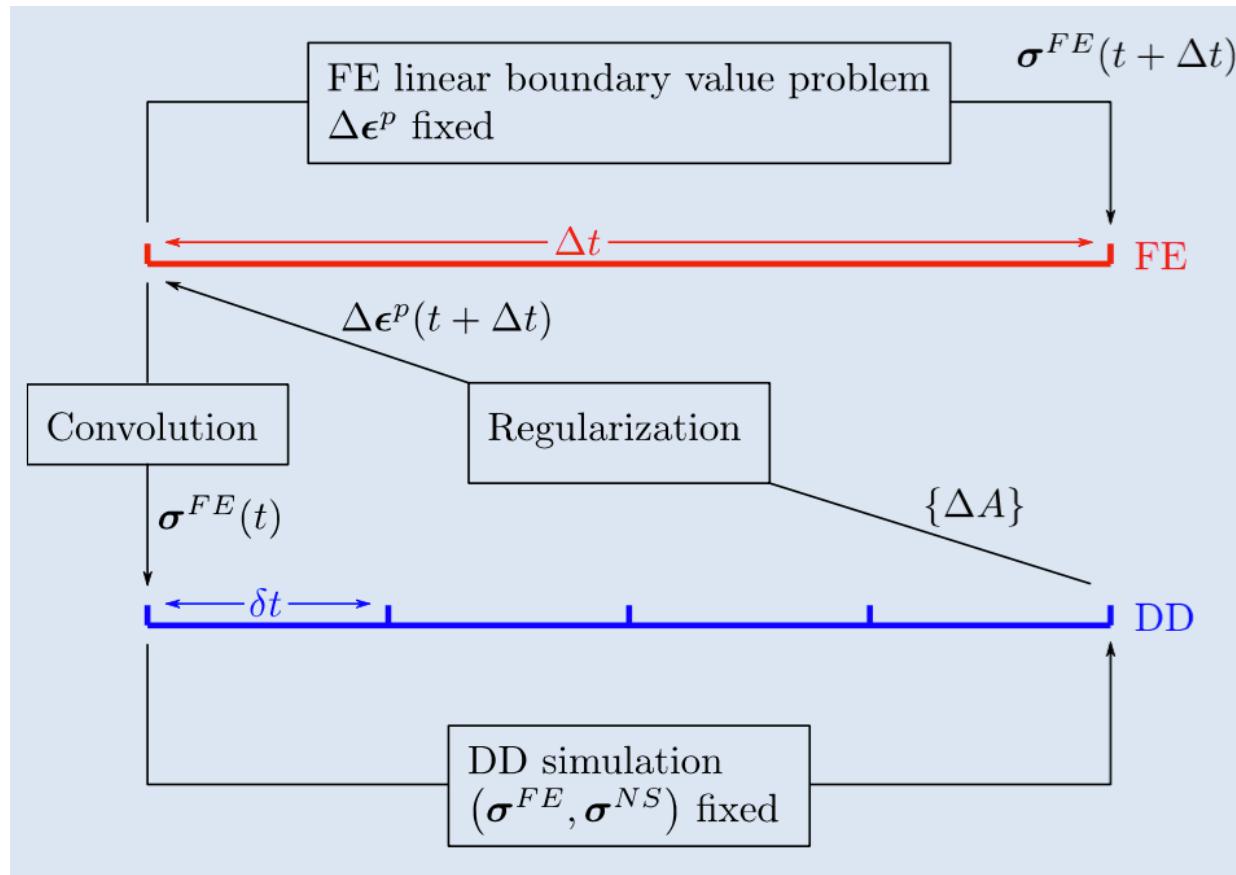
Stress field



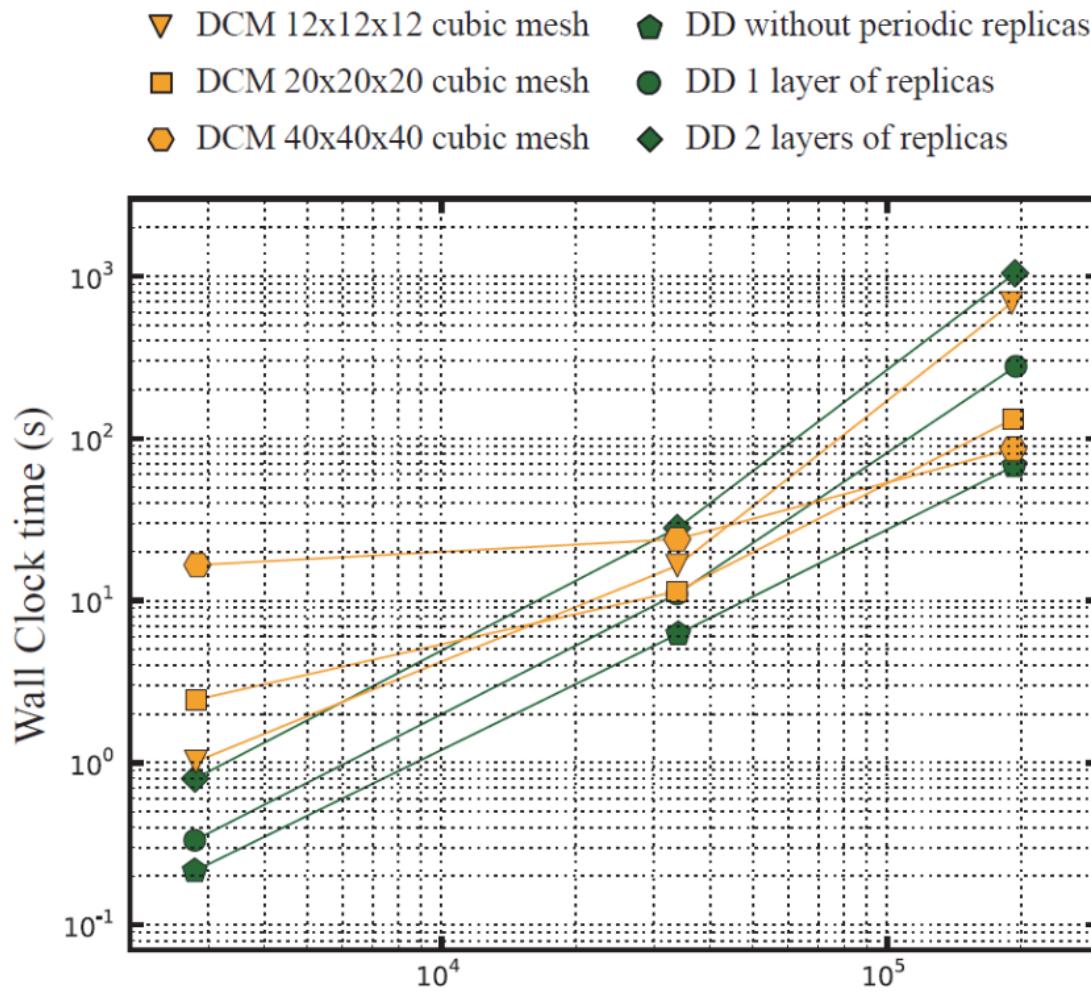
Complex domains

# Time integration algorithm

- Linear elasticity problem
- Forward Euler (explicite)
- Two time steps



# DCM performance



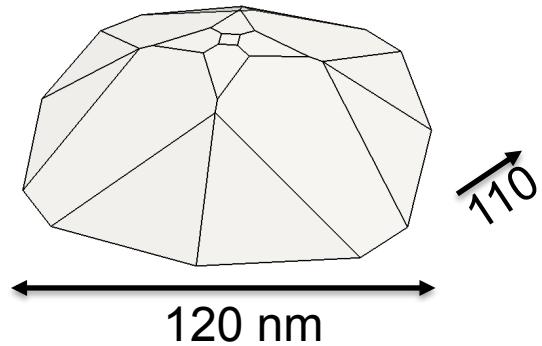
- Periodic system
- DD computations: FMM algorithm, 12 proc MPI
- DCMcomputations : 12 proc MPI, 12 Proc FEM multithread, time step ratio=1
- 24 x X5670 2.9 GHz Xeon CPU

At large number of segments and with a fine mesh, the DCM becomes faster than standard DD simulation codes with the FMM algorithm.

# DCM simulation exemples

# Plastic deformation in nano-objects

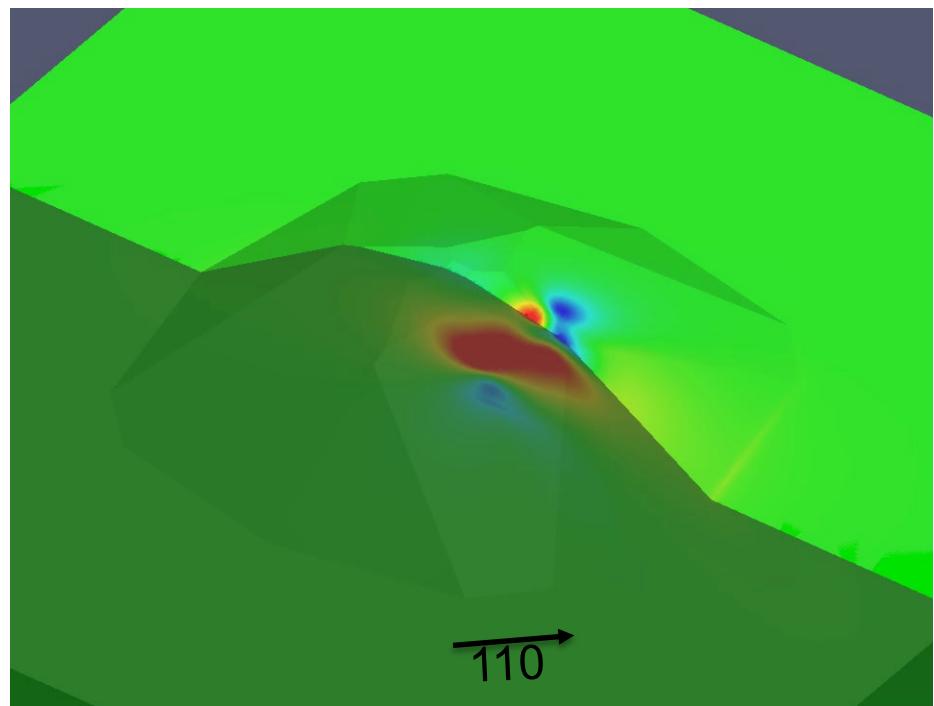
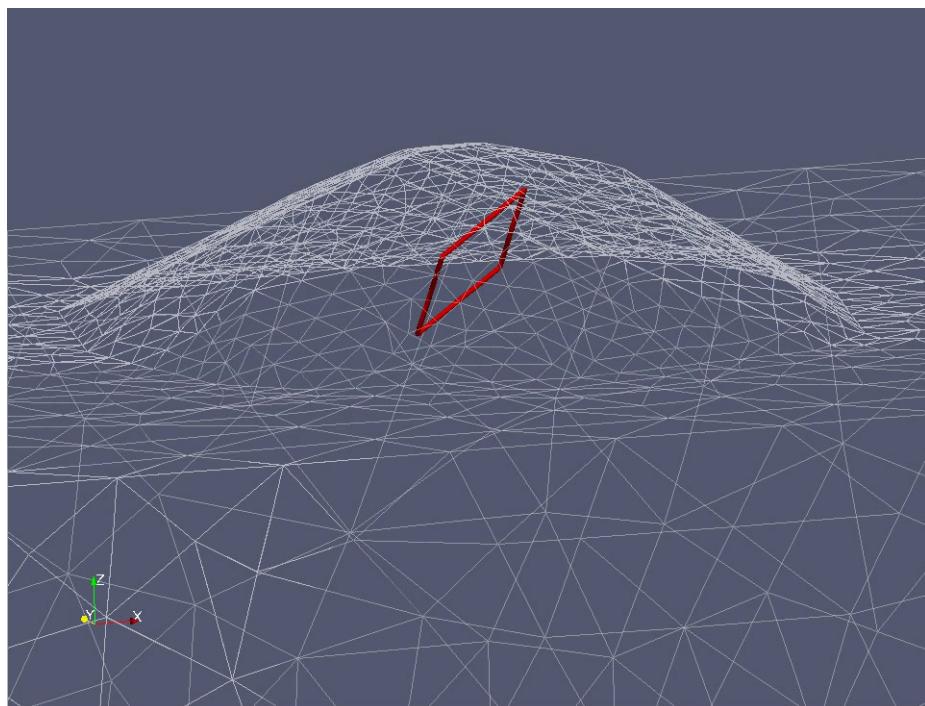
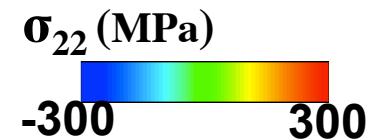
**SiGe self-assembled island**



Ge content = 0.4

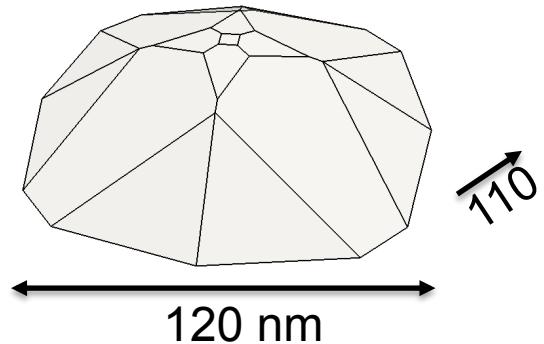
Anisotropic elastic constant

$h= 5 \text{ nm}$



# Plastic deformation in nano-objects

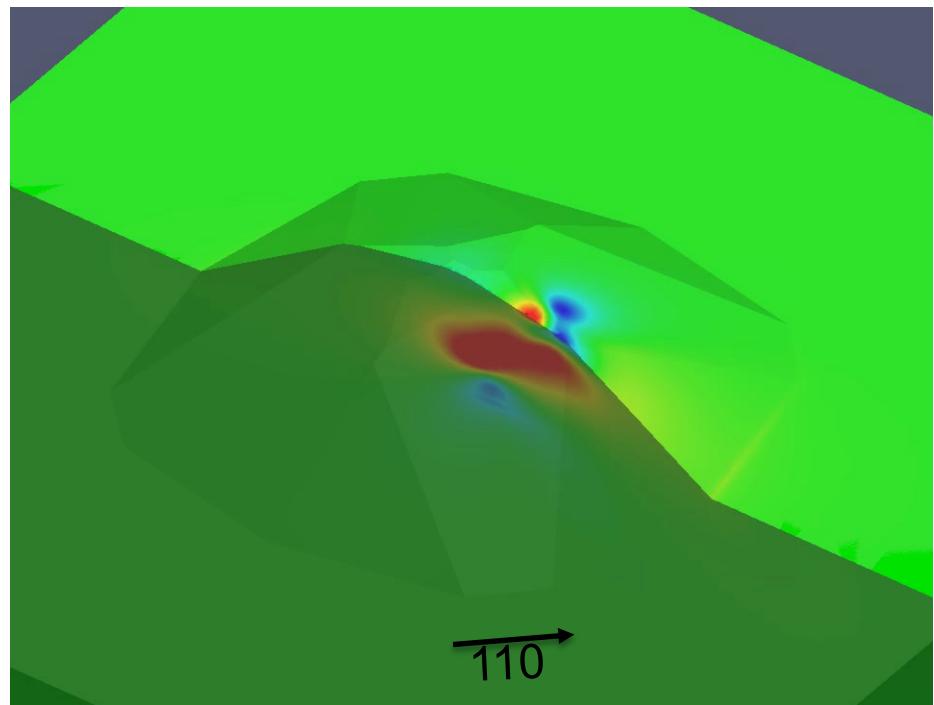
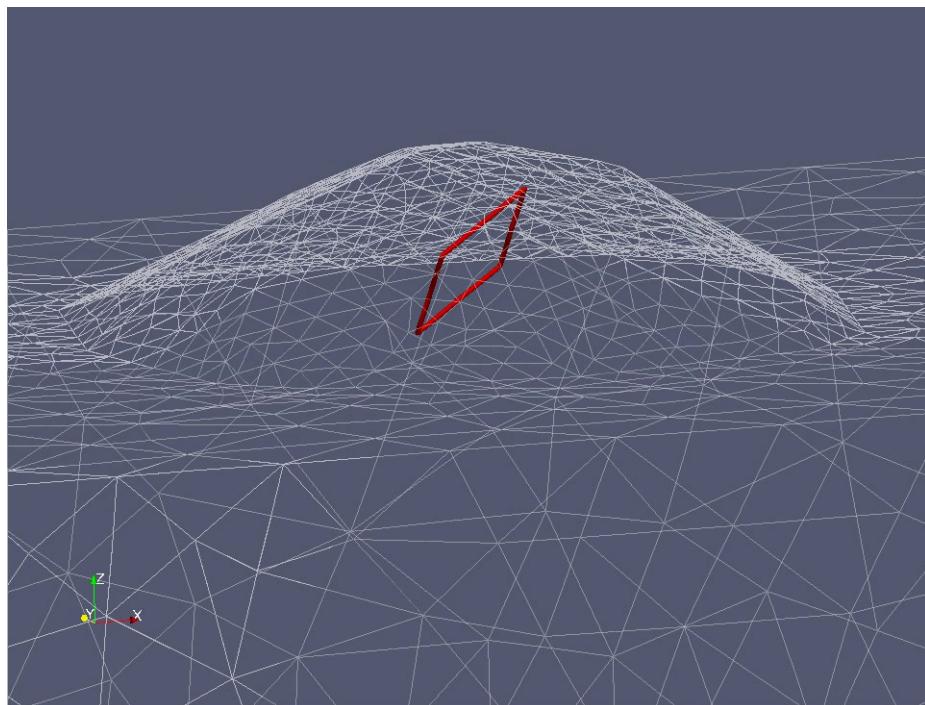
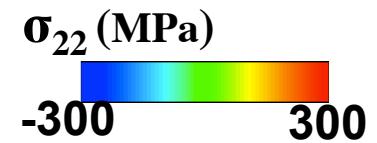
SiGe self-assembled island



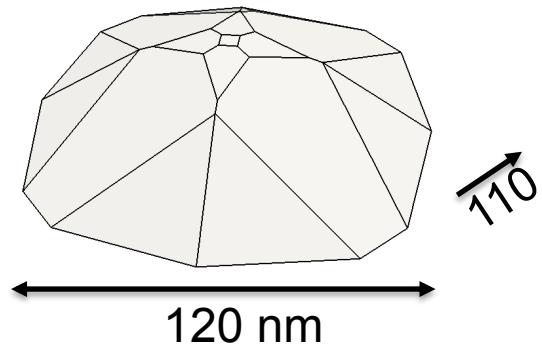
Ge content = 0.4

Anisotropic elastic constant

$h= 5 \text{ nm}$



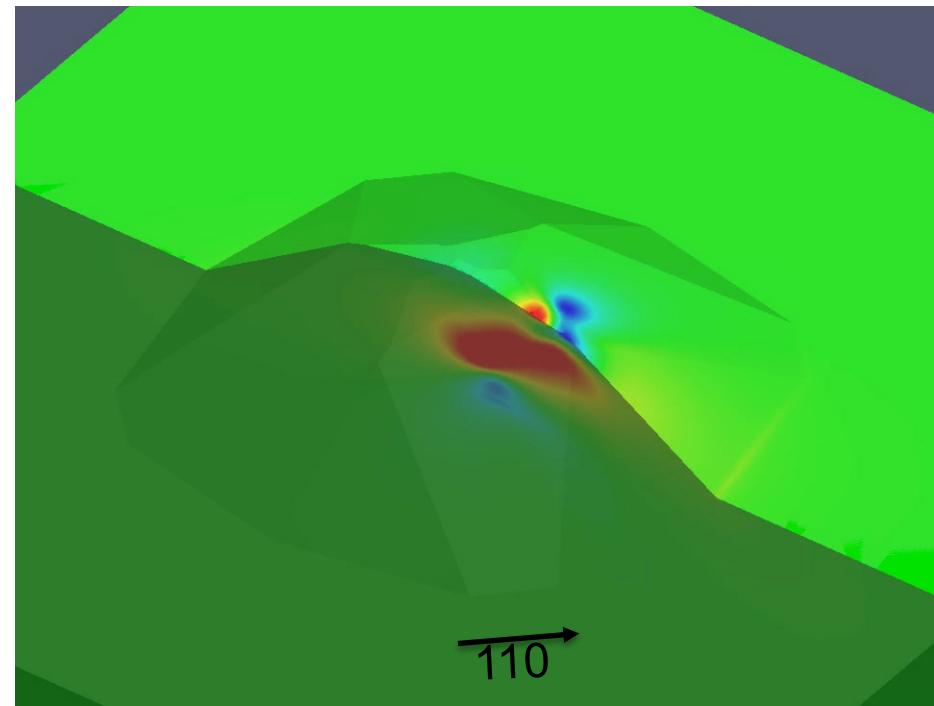
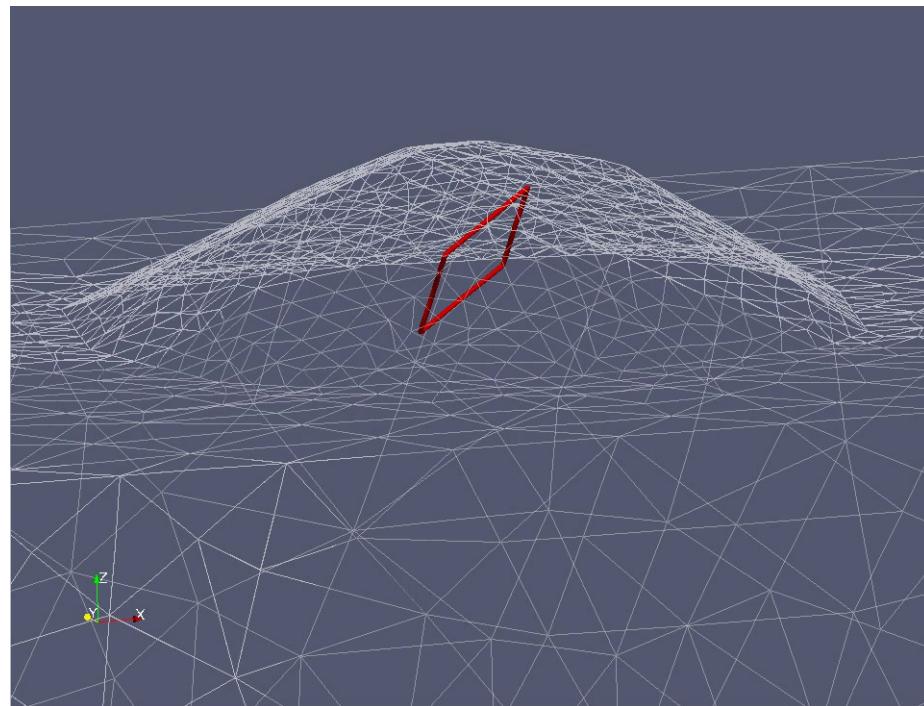
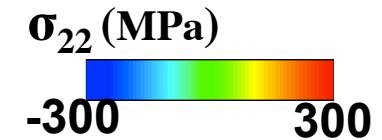
# Plastic deformation in nano-objects



Ge content = 0.4

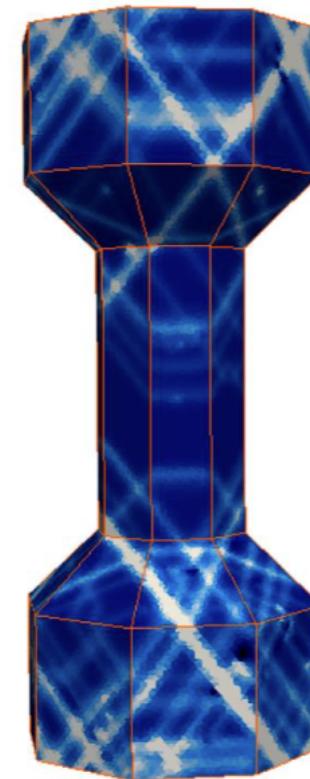
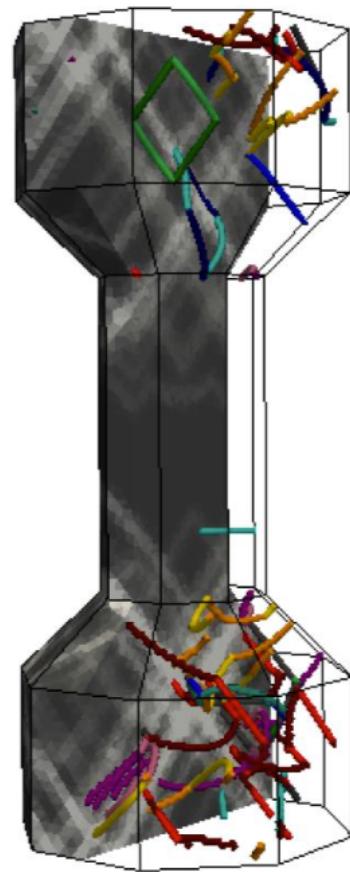
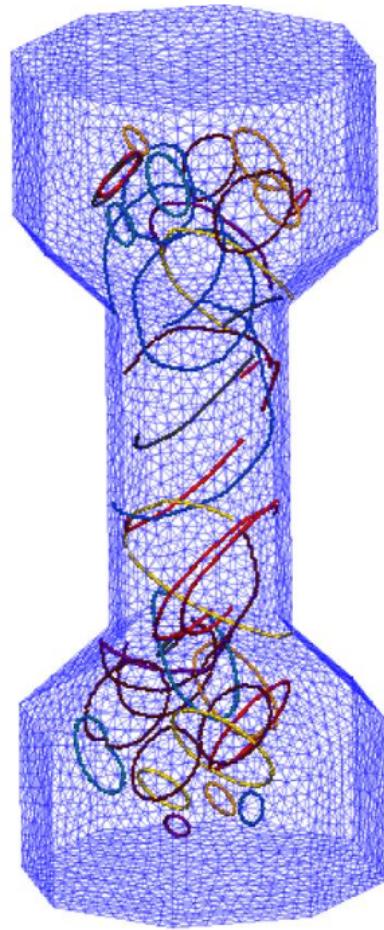
Anisotropic elastic constant

$h= 5 \text{ nm}$



No local correction to study nano-objects (100 nm -500 nm)

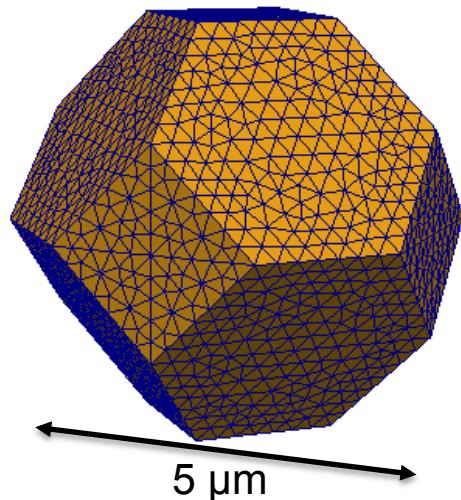
# Deformation test on a micro-sample (D=0.5μm)



# DD + Crystal Plasticity

Cu polycrystal plastic deformation

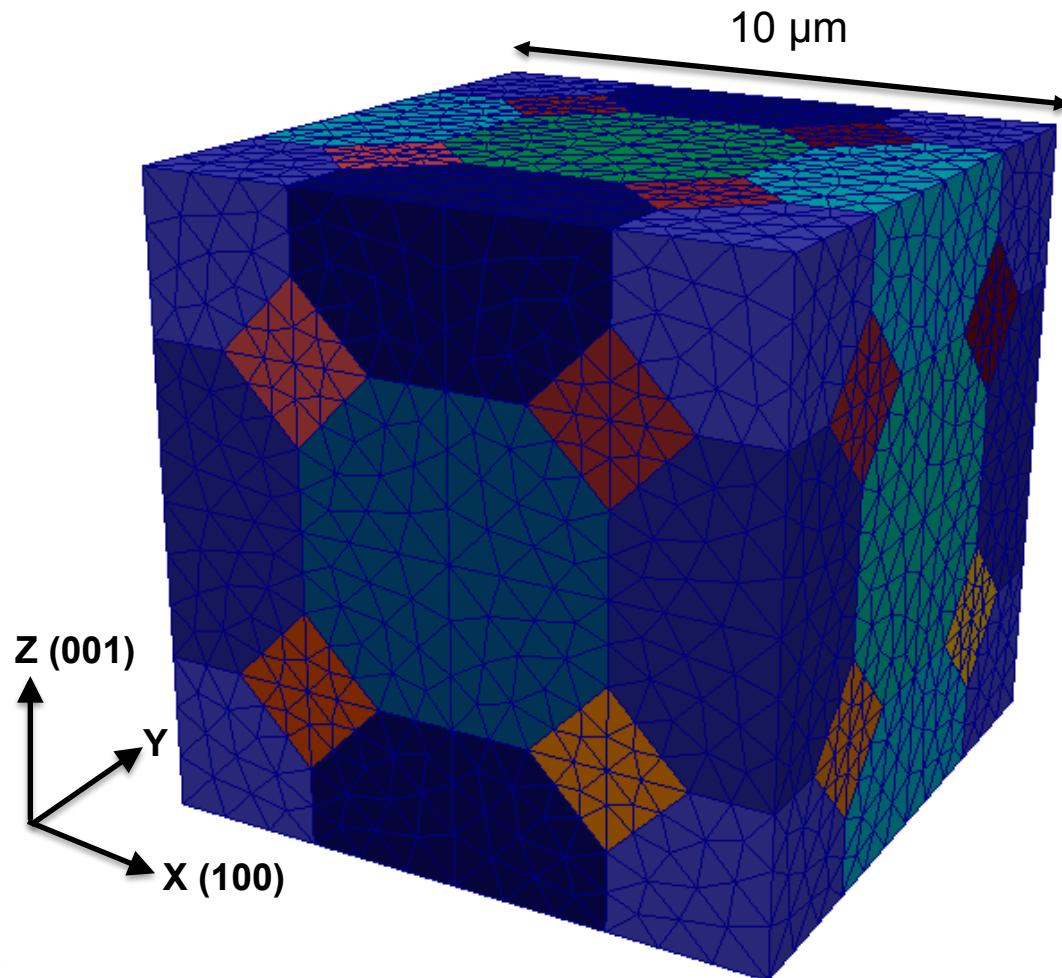
Grain shape



(111) and (001) boundaries

- 1 DCM grain oriented following x, y, z axis (central grain)
- 15 Crystal Plasticity grain randomly oriented

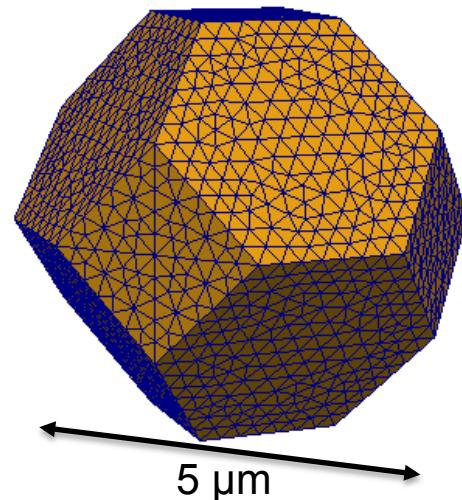
FE Mesh (16 grains)



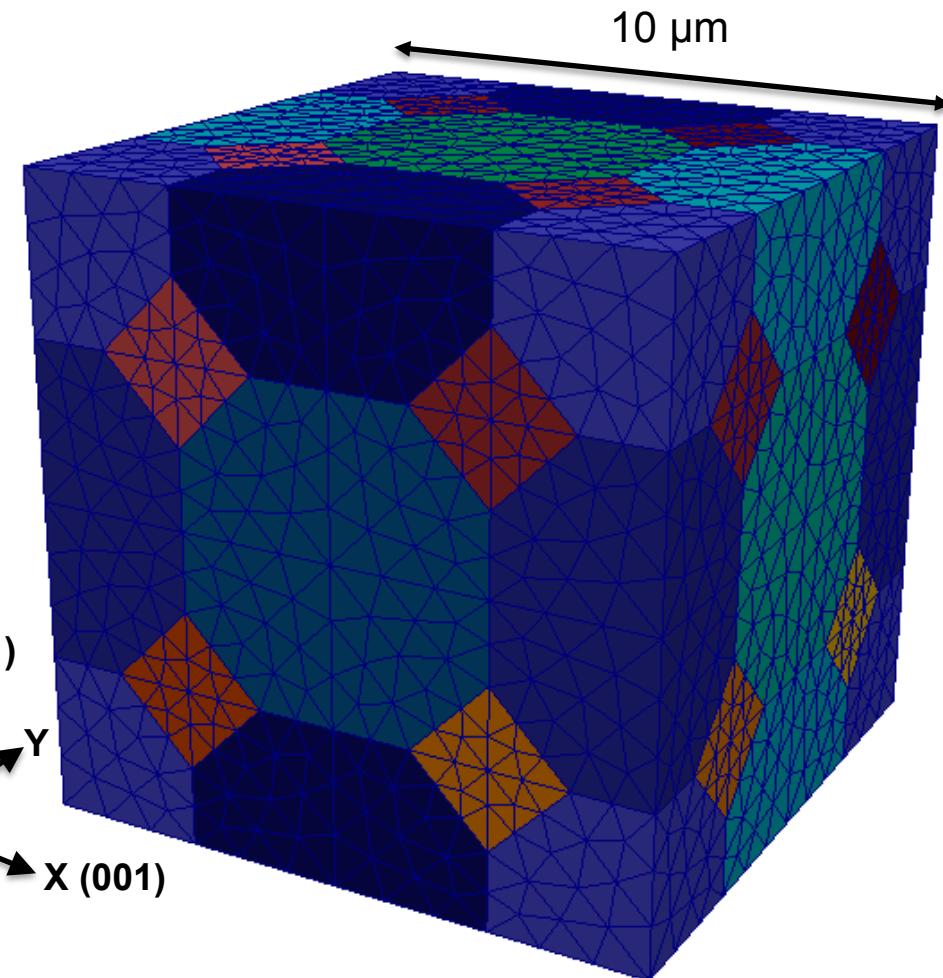
# DD + Crystal Plasticity

Cu polycrystal plastic deformation

Grain shape



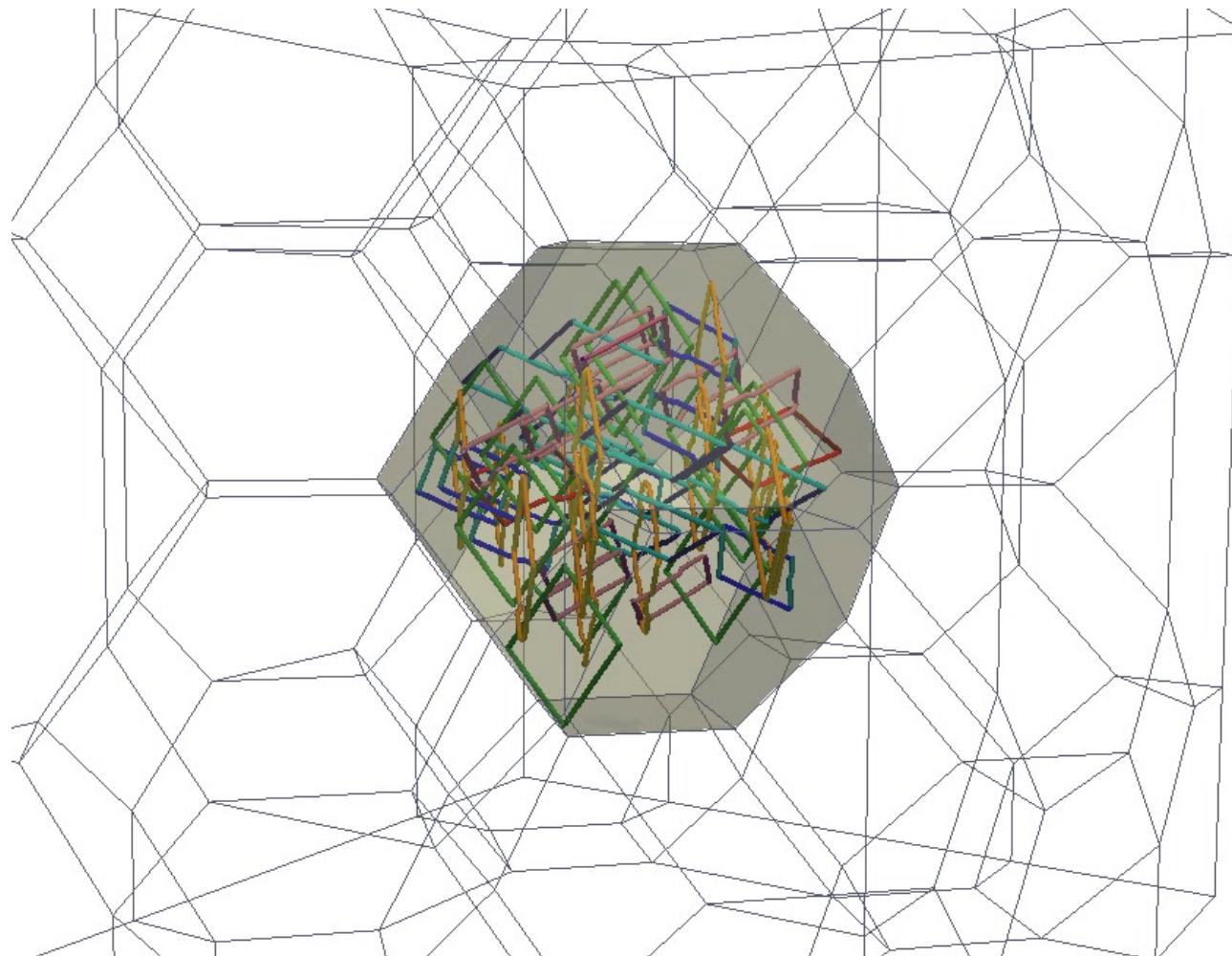
FE Mesh (16 grains)



- Periodic boundary condition in X, Y, Z direction
- uniaxial loading in Z direction
- Strain rate  $10^2 \text{ s}^{-1}$
- dislocation density  $3 \times 10^{12} \text{ m}^{-2}$

# DD + Crystal Plasticity

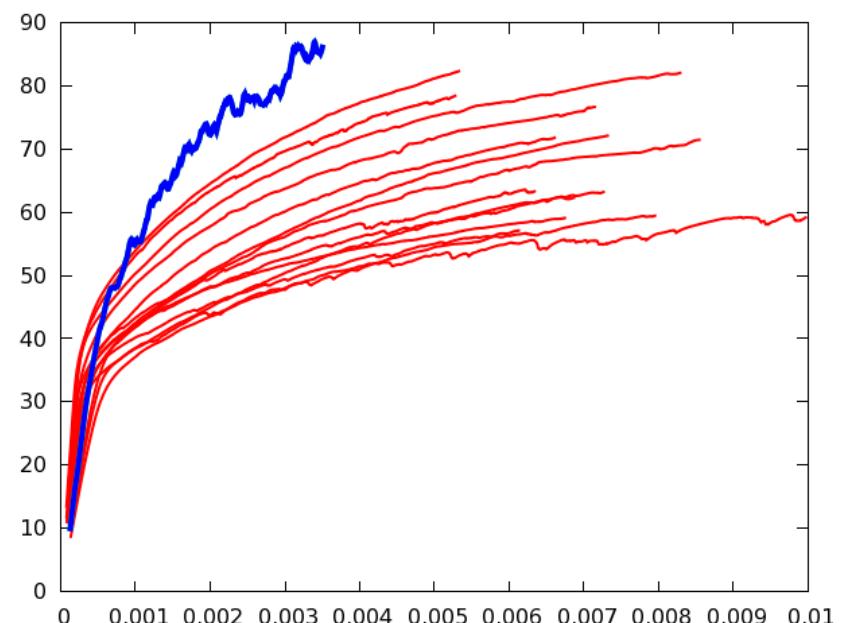
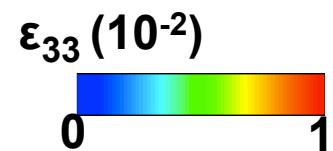
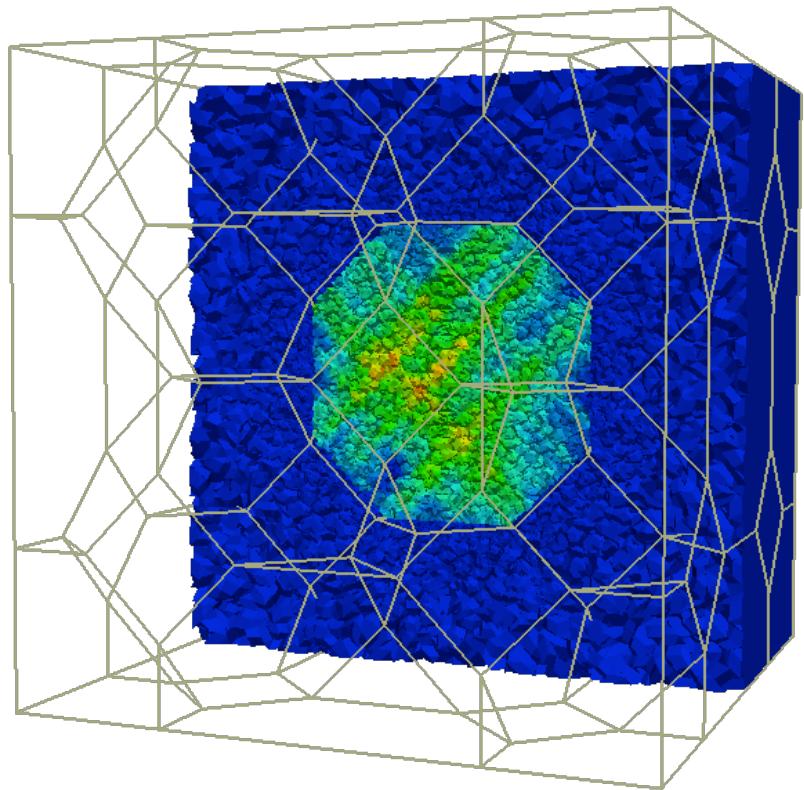
Cu polycrystal plastic deformation



# DD + Crystal Plasticity

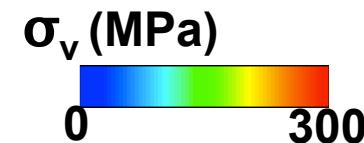
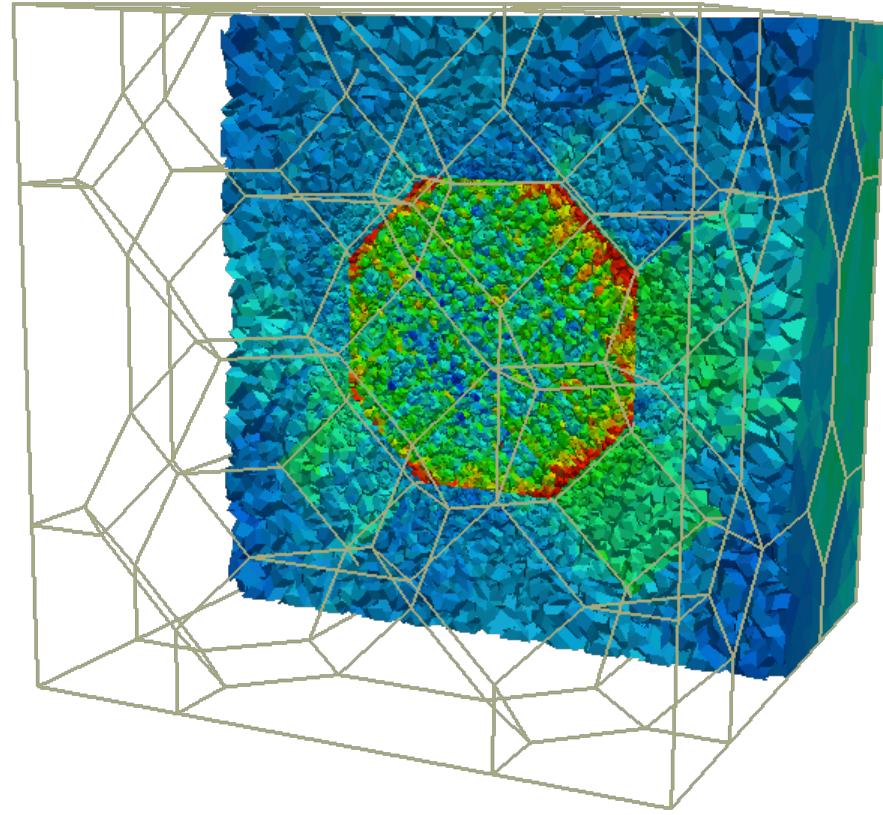
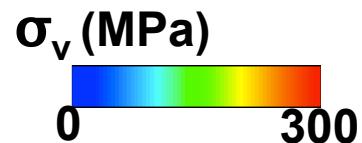
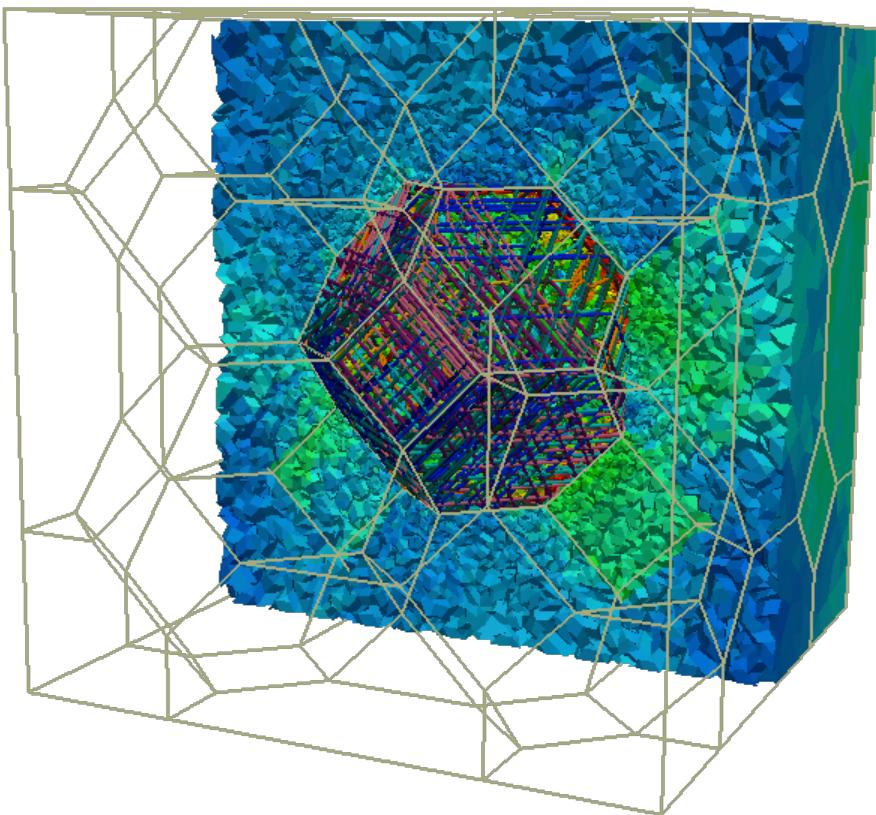
Cu polycrystal plastic deformation

DCM grain



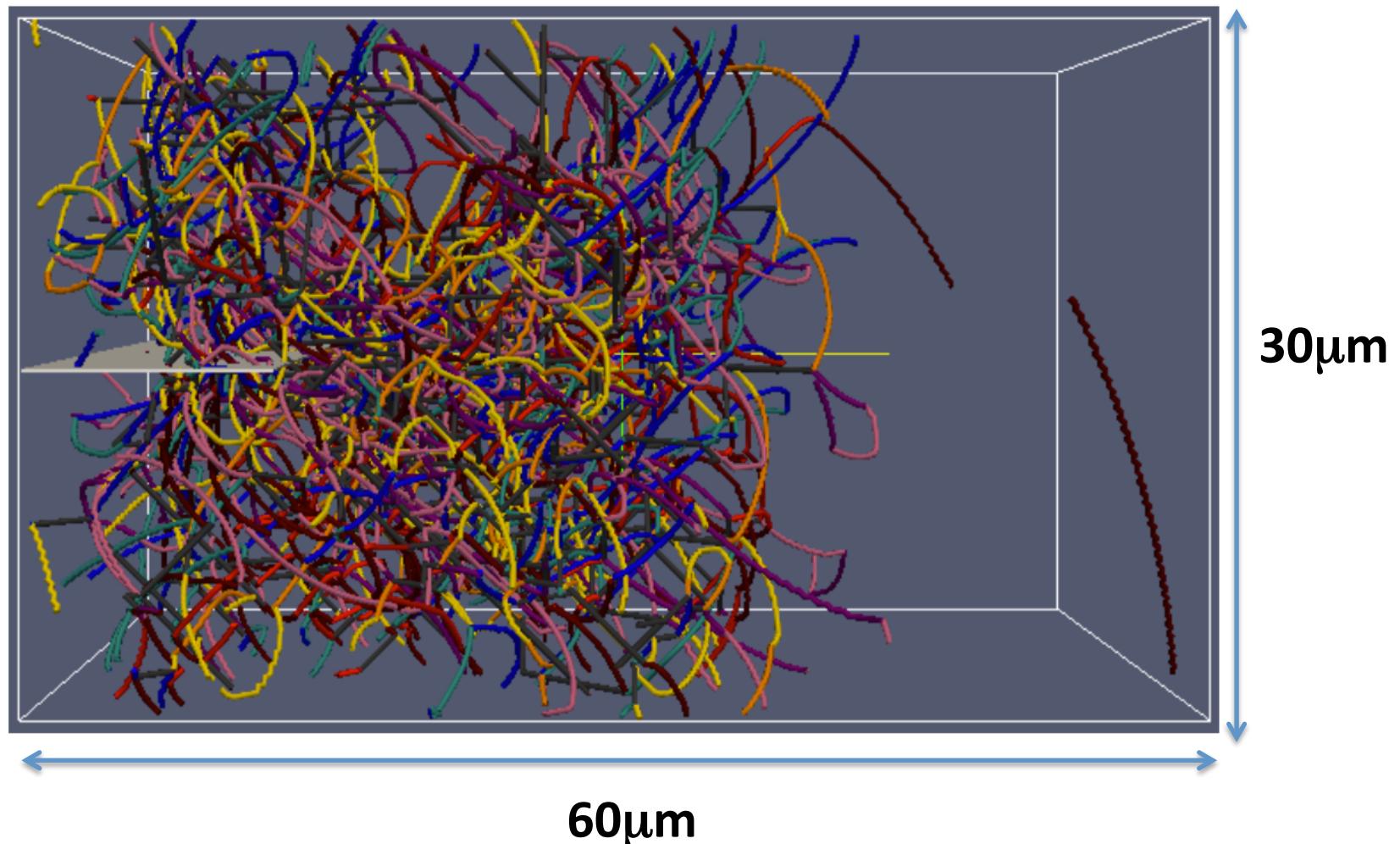
# DD + Crystal Plasticity

Cu polycrystal plastic deformation

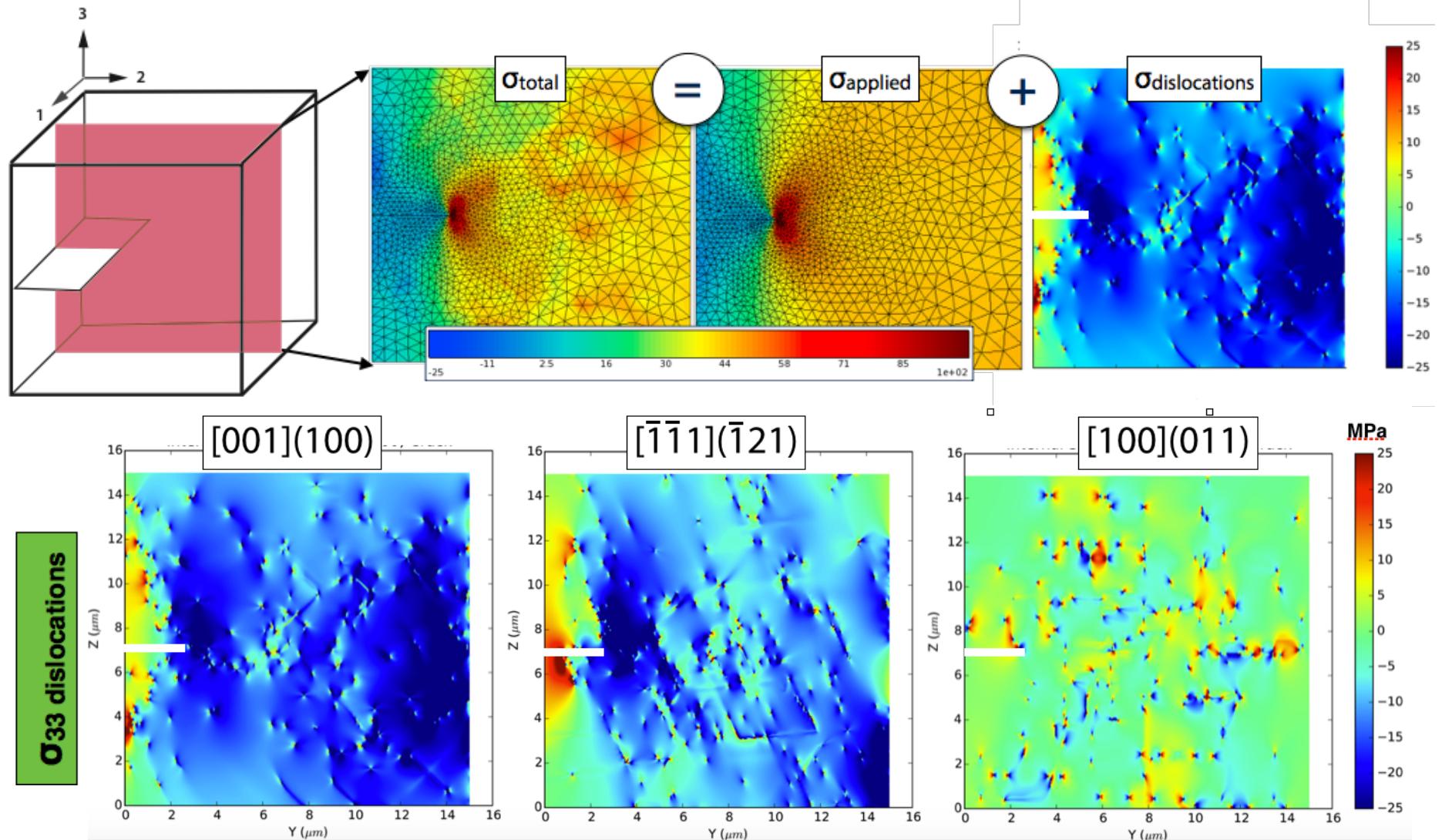


# 3D dislocation-crack interactions

PhD L. Korzeczek (2013-2016)



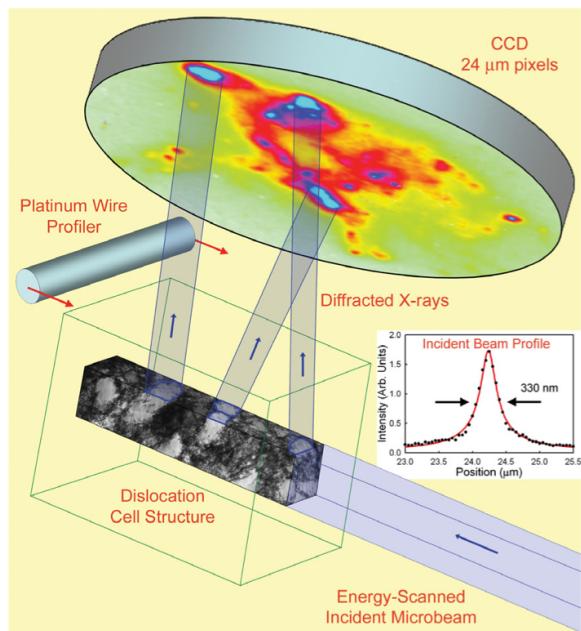
# 3D Crack Shielding and Blunting



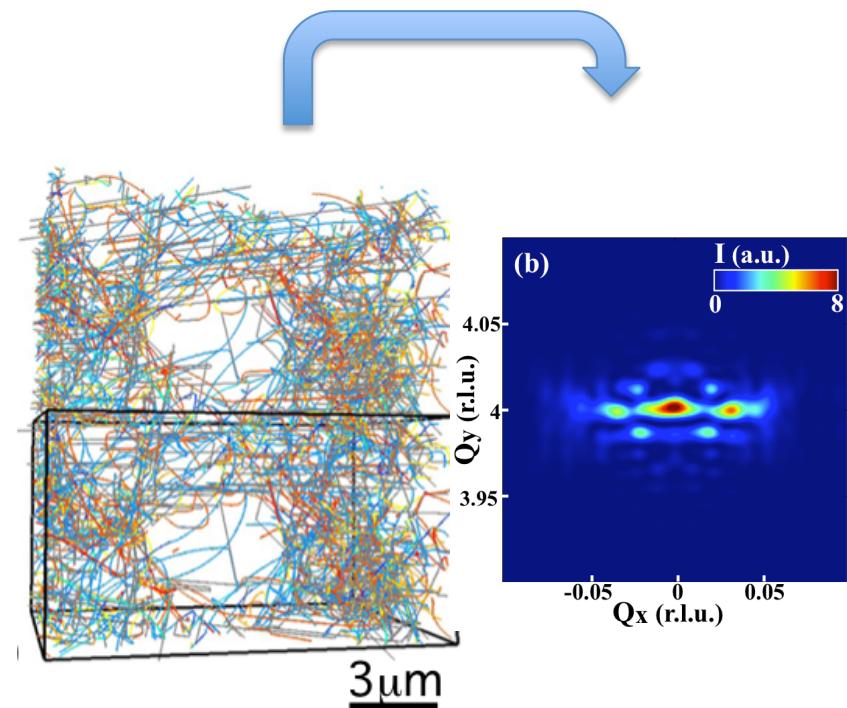
# $\mu$ -XRD simulations

Synchrotron recent improvements

*Coll. P. Geantil et M. Kassner (Univ Cal.)*



XRD simulation with the DCM



# Concluding remarks

We revised The Discrete Continuum Model (DCM) :

- A new regularization procedure to improve the treatment of short range interaction between dislocations has been introduced
- The possibility of handling unstructured meshes was included in order to run simulation in complex domains
- Performances were improved



The DCM is a unique and powerful tool to investigate, in a physically justified manner, 3D micro-mechanics problems!

# **MMM2016**

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The organizing committee:

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